

# Aerodynamic Optimisation of Aerofoils for Martian Rotorcraft



ERCOFTAC, 10<sup>th</sup> October 2024

---

LIDIA CARÓS ROCA

PHD CANDIDATE, IMPERIAL COLLEGE LONDON

PROF. PETER VINCENT

PROF. OLIVER BUXTON

# Outline

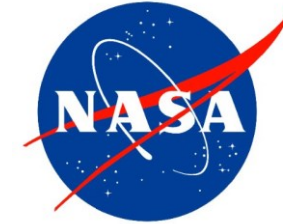
- Introduction
- Optimisation setup
- Optimisation results
- Effects of free-stream eddies
- Summary and future work

# Outline

- Introduction
- Optimisation setup
- Optimisation results
- Effects of free-stream eddies
- Summary and future work

# Introduction - Motivation

Ingenuity achieved first powered flight on another planet (Mars) on 2021



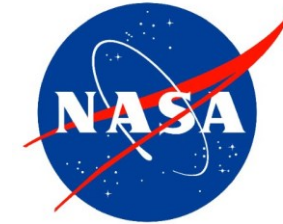
Technology demonstrator – 5 planned flights  
Flew from April 2021 to January 2024  
72 flights - Covered 17 km



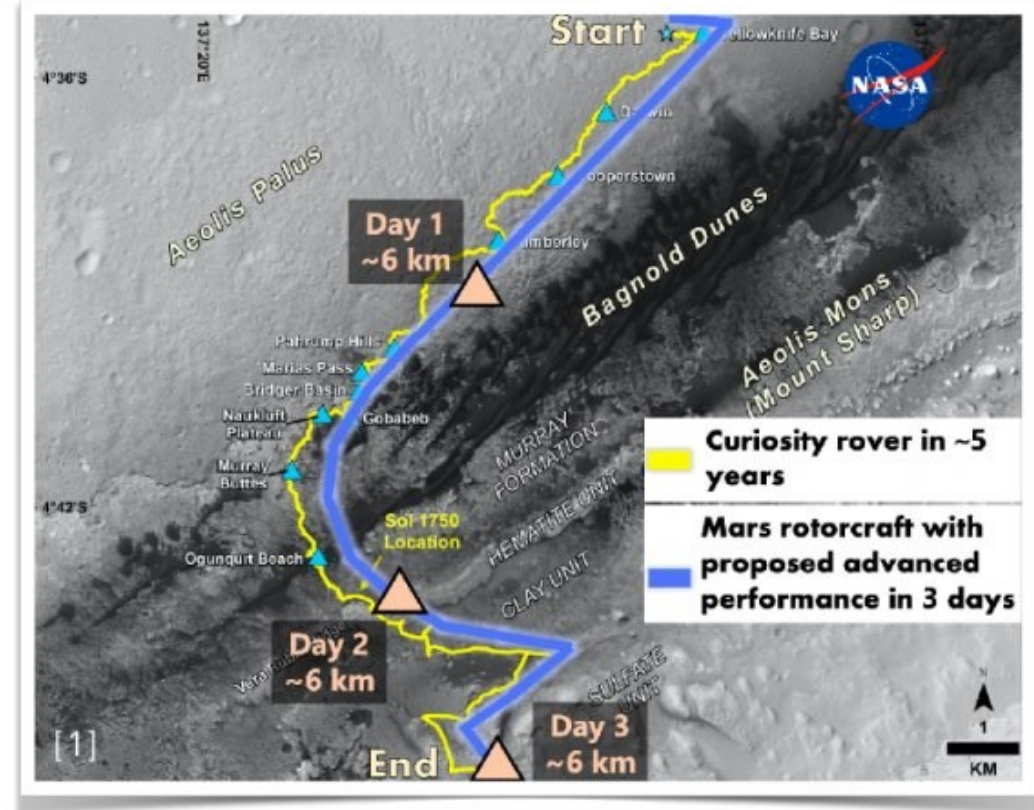
<https://mars.nasa.gov/technology/helicopter>

# Introduction - Motivation

Next-generation Martian helicopter for science and discovery



Increased payload – science equipment  
 Increased range – exploration beyond rovers



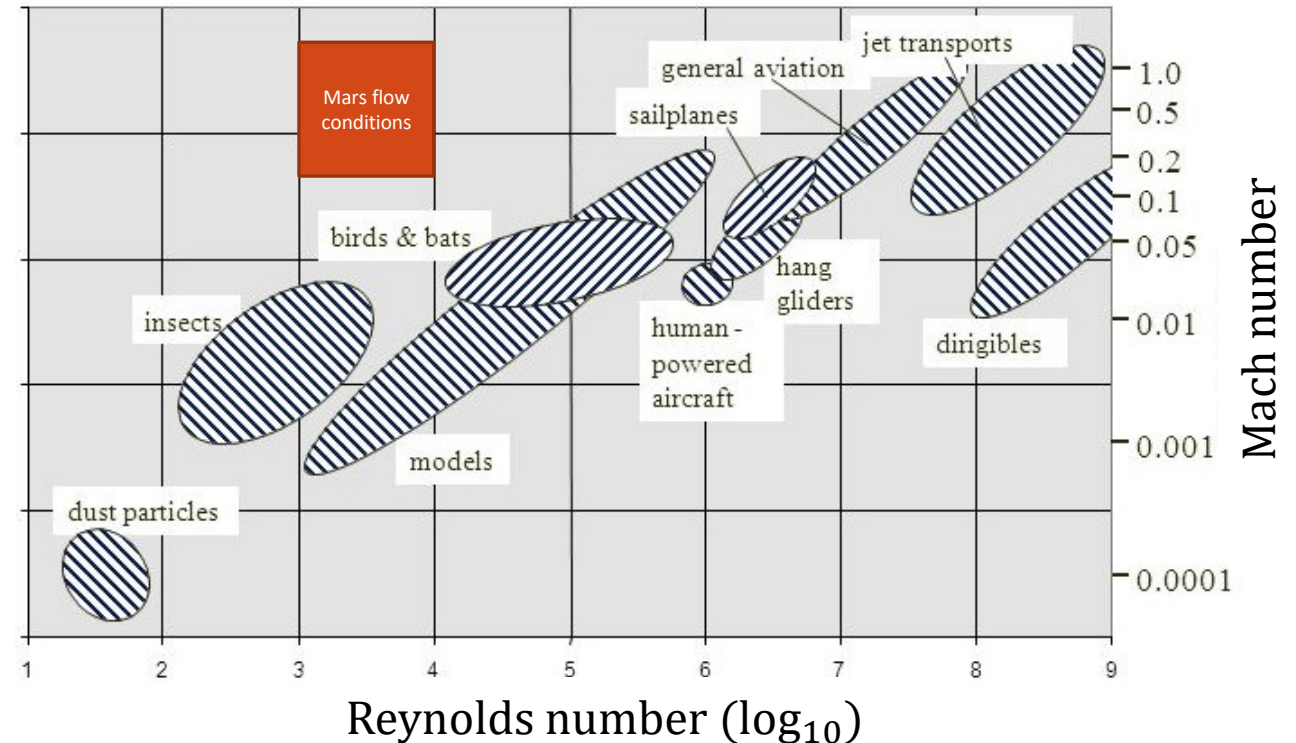
# Introduction - Martian atmospheric conditions

Designing airfoils for Martian Rotorcraft is challenging due to the flow conditions on Mars of very low density and low speed of sound:

Low Reynolds Number ( $10^3 - 10^4$ )

Compressible Mach Number (0.7 - 0.9)

- Years of research have optimised airfoils for all flow conditions on Earth
- Martian rotorcraft airfoils is a reasonably unexplored field



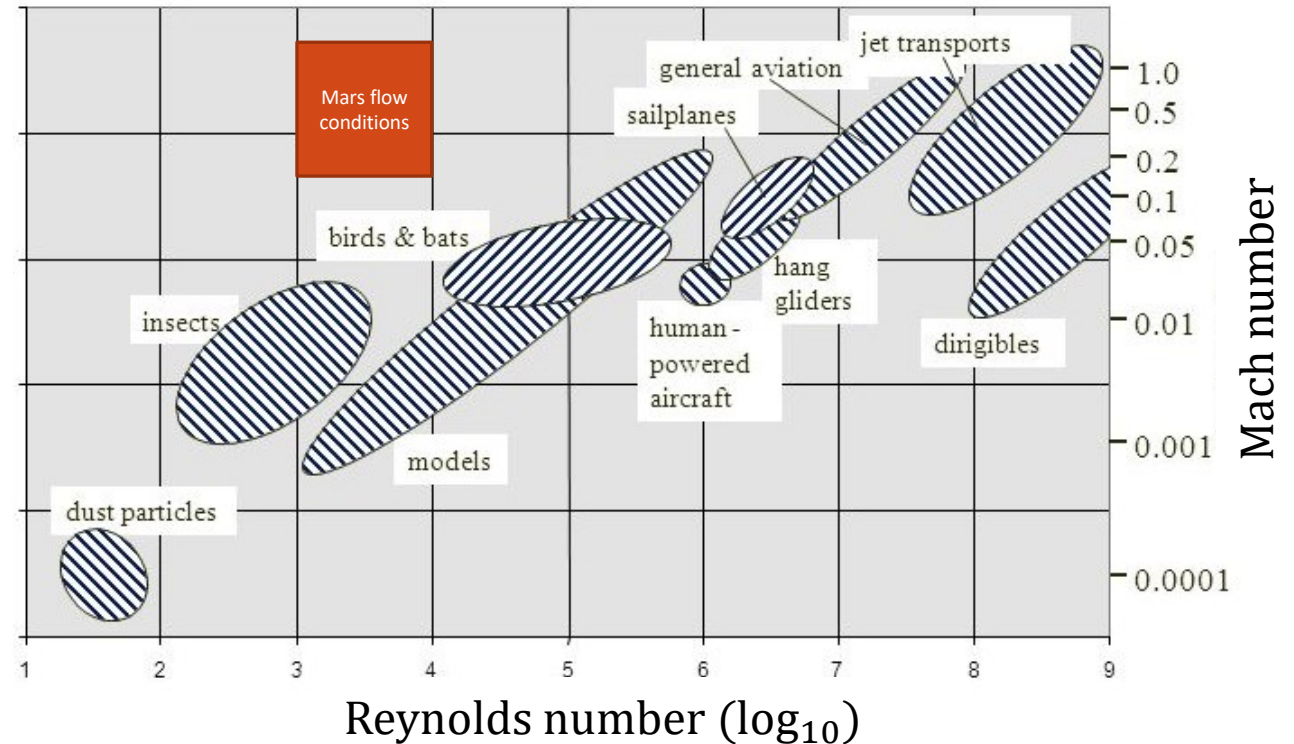
# Introduction - Martian atmospheric conditions

Designing airfoils for Martian Rotorcraft is challenging due to the flow conditions on Mars of very low density and low speed of sound:

Low Reynolds Number ( $10^3 - 10^4$ )

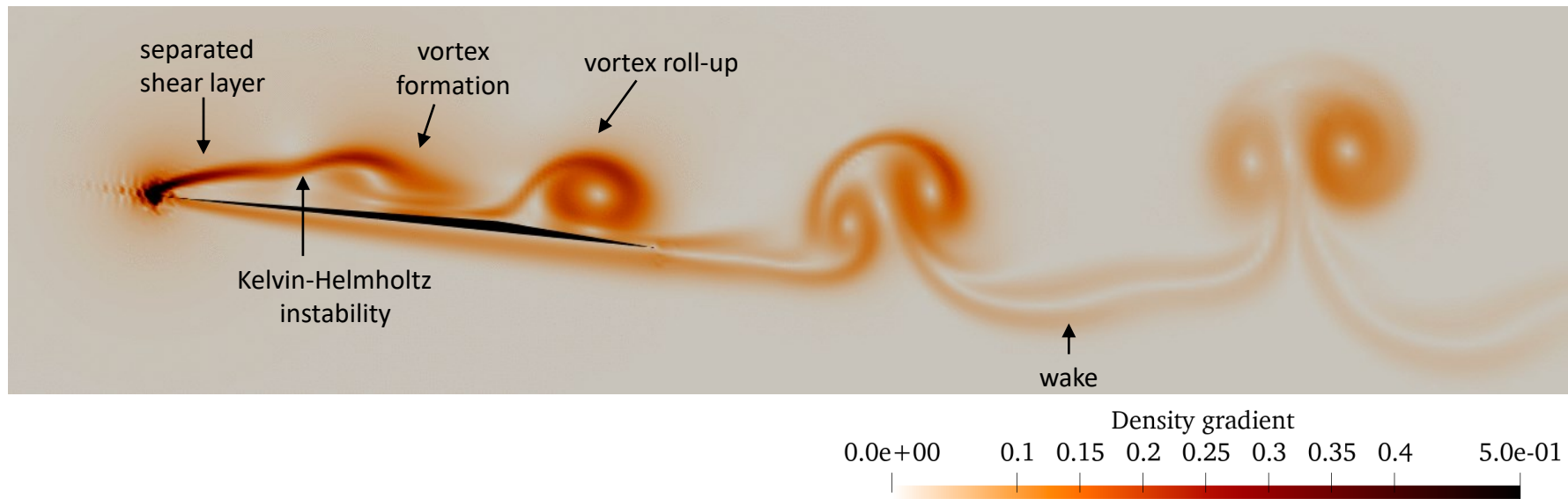
Compressible Mach Number (0.7 - 0.9)

- Years of research have optimised airfoils for all flow conditions on Earth
- Martian rotorcraft airfoils is a reasonably unexplored field



# Introduction - Sharp-leading-edge airfoils

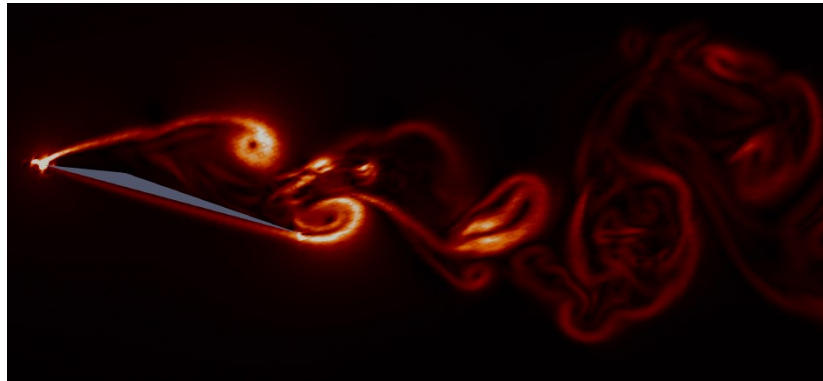
- Separated flow from the sharp leading edge
- Separated shear layer ondulates
- Formation of large coherent vortices (roll-up)
- Flow unsteadiness





# Introduction - Optimisation of sharp-leading-edge airfoils

## Unsteady and transitional flow - DNS

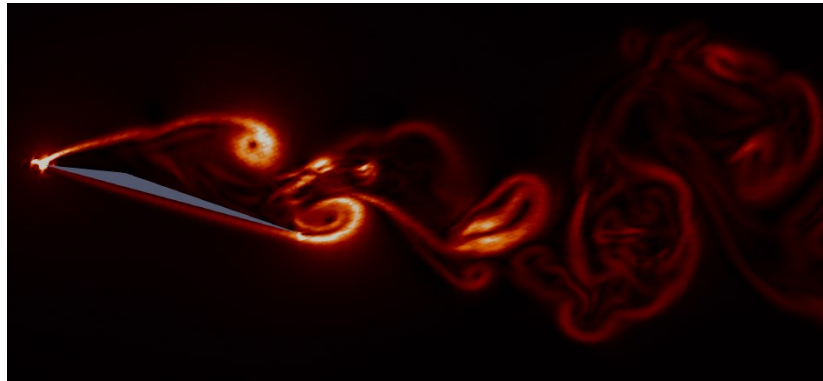


F. D. Witherden, A. M. Farrington, and P. E. Vincent. **PyFR**: An open source framework for solving advection-diffusion type problems on streaming architectures using the flux reconstruction approach. *Computer Physics Communications*, 185(11):3028–3040, 2014.

J. Blank and K. Deb, **pymoo**: Multi-Objective Optimisation in Python, in *IEEE Access*, vol. 8, pp. 89497-89509, 2020, 10.1109/ACCESS.2020.2990567

# Introduction - Optimisation of sharp-leading-edge airfoils

## Unsteady and transitional flow - DNS



### Direct Numerical Simulations

- High order accurate
- Unstructured meshes
- High parallel performance
- GPU-enabled

F. D. Witherden, A. M. Farrington, and P. E. Vincent. **PyFR**: An open source framework for solving advection-diffusion type problems on streaming architectures using the flux reconstruction approach. *Computer Physics Communications*, 185(11):3028–3040, 2014.

J. Blank and K. Deb, **pymoo**: Multi-Objective Optimisation in Python, in *IEEE Access*, vol. 8, pp. 89497-89509, 2020, 10.1109/ACCESS.2020.2990567

# Introduction - Optimisation of sharp-leading-edge airfoils

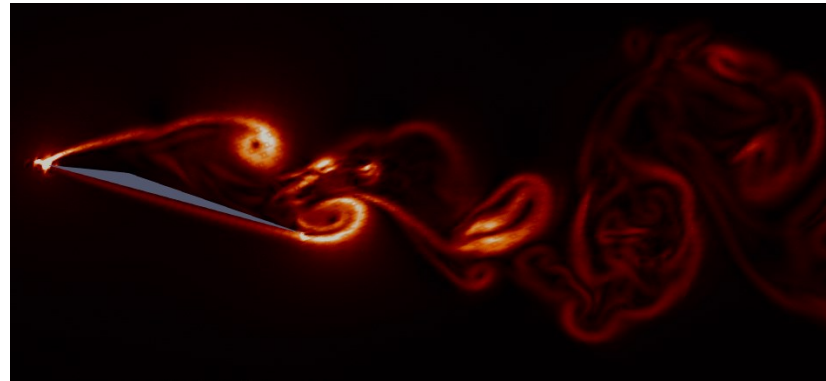


pymoo

## Genetic Algorithms

- No gradient information needed
- Avoid local optima
- Easy to parallelize

## Unsteady and transitional flow - DNS



PyFR

## Direct Numerical Simulations

- High order accurate
- Unstructured meshes
- High parallel performance
- GPU-enabled

F. D. Witherden, A. M. Farrington, and P. E. Vincent. **PyFR**: An open source framework for solving advection-diffusion type problems on streaming architectures using the flux reconstruction approach. *Computer Physics Communications*, 185(11):3028–3040, 2014.

J. Blank and K. Deb, **pymoo**: Multi-Objective Optimisation in Python, in *IEEE Access*, vol. 8, pp. 89497-89509, 2020, 10.1109/ACCESS.2020.2990567

# Introduction - Optimisation of sharp-leading-edge airfoils



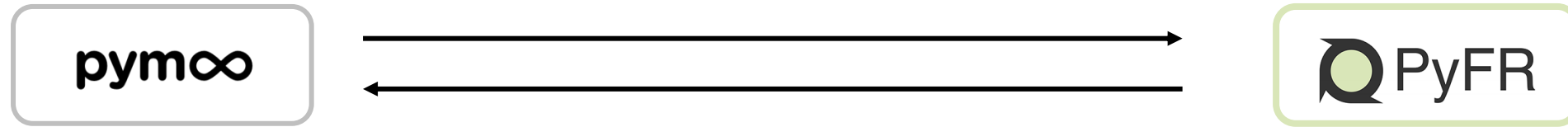
F. D. Witherden, A. M. Farrington, and P. E. Vincent. **PyFR**: An open source framework for solving advection-diffusion type problems on streaming architectures using the flux reconstruction approach. *Computer Physics Communications*, 185(11):3028–3040, 2014.

J. Blank and K. Deb, **pymoo**: Multi-Objective Optimisation in Python, in *IEEE Access*, vol. 8, pp. 89497-89509, 2020, 10.1109/ACCESS.2020.2990567

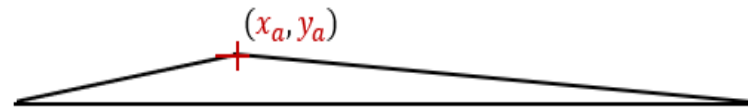
# Outline

- Introduction
- **Optimisation setup**
- Optimisation results
- Effects of free-stream eddies
- Summary and future work

## Optimisation setup



Design variables

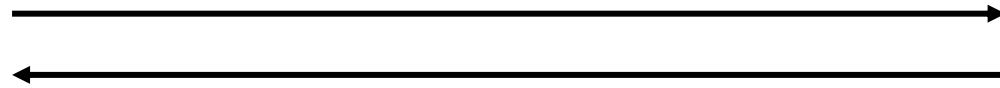


Apex coordinates of a triangular airfoil at  
angle of attack of  $\alpha = 12^\circ$

$Re = 3,000$  and  $M = 0.15$

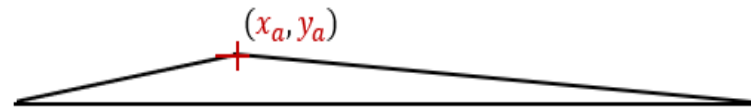
# Optimisation setup

pymoo



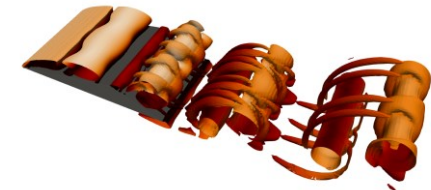
PyFR

Design variables



Evaluation

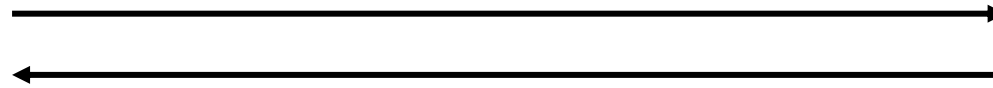
3D DNS with span 0.6c



Apex coordinates of a triangular airfoil at angle of attack of  $\alpha = 12^\circ$

Re = 3,000 and M = 0.15

# Optimisation setup



Objective functions

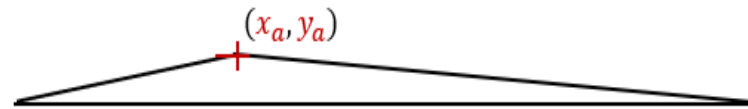
CL and CD

Multi-objective optimisation



Multiple optimum solutions

Design variables

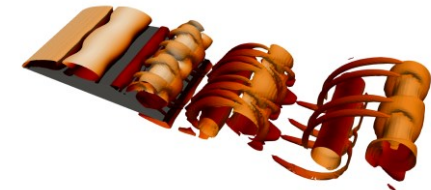


Apex coordinates of a triangular airfoil at angle of attack of  $\alpha = 12^\circ$

Re = 3,000 and M = 0.15

Evaluation

3D DNS with span 0.6c





# Optimisation setup

pymoo

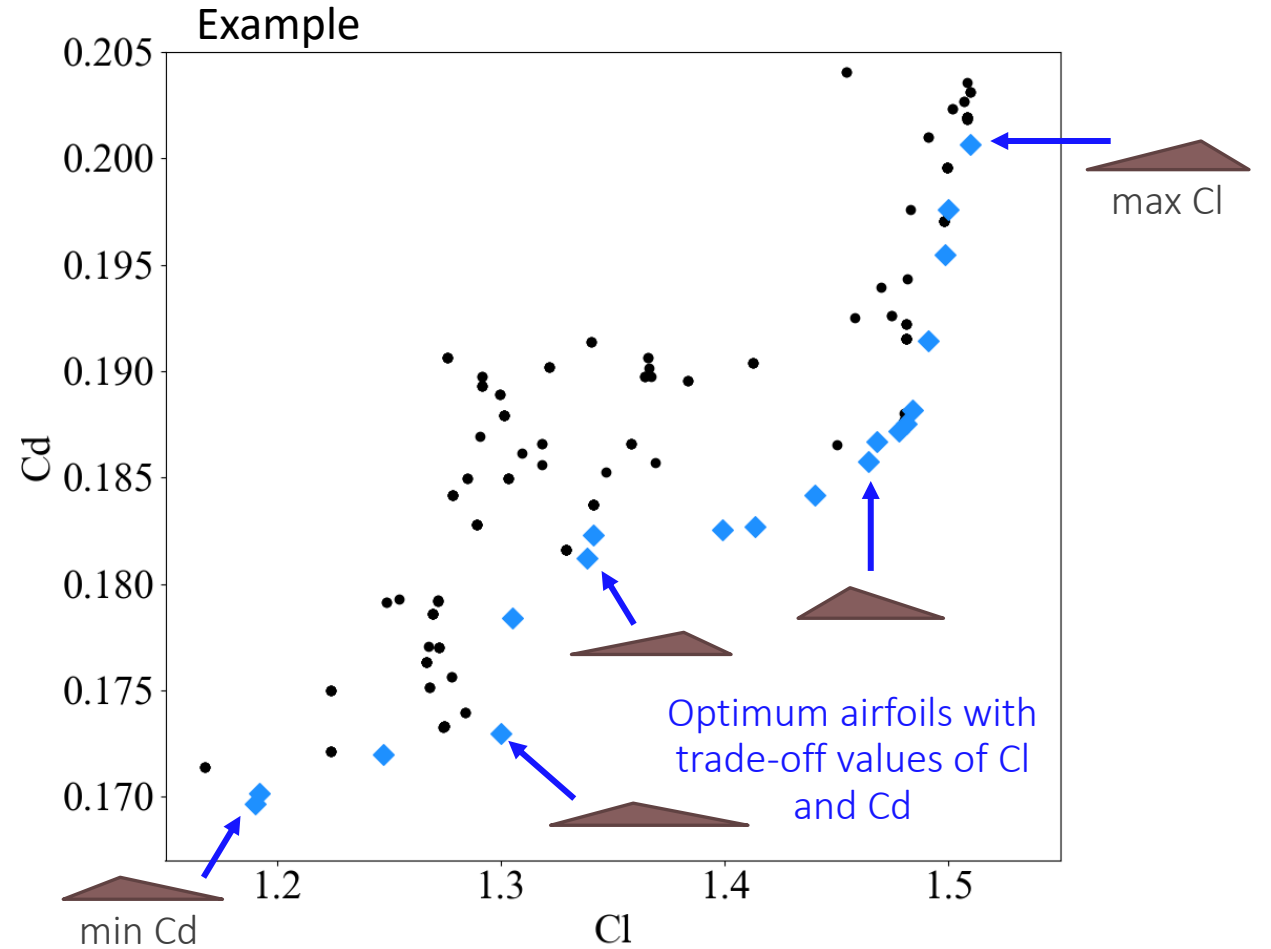
Objective functions

CL and CD

Multi-objective optimisation



Multiple optimum solutions



# Optimisation setup

pymoo

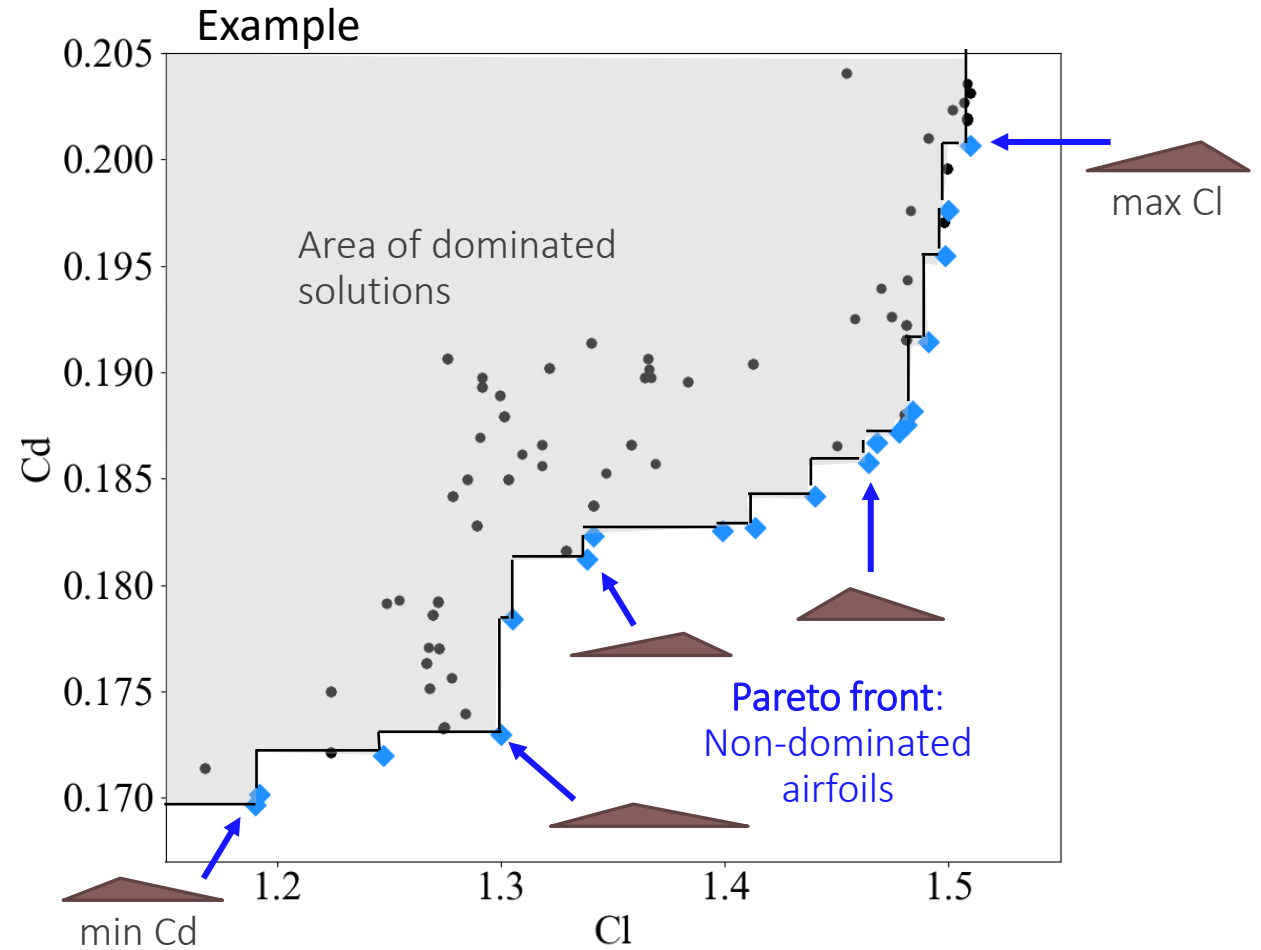
## Objective functions

CL and CD

Multi-objective optimisation



Multiple optimum solutions



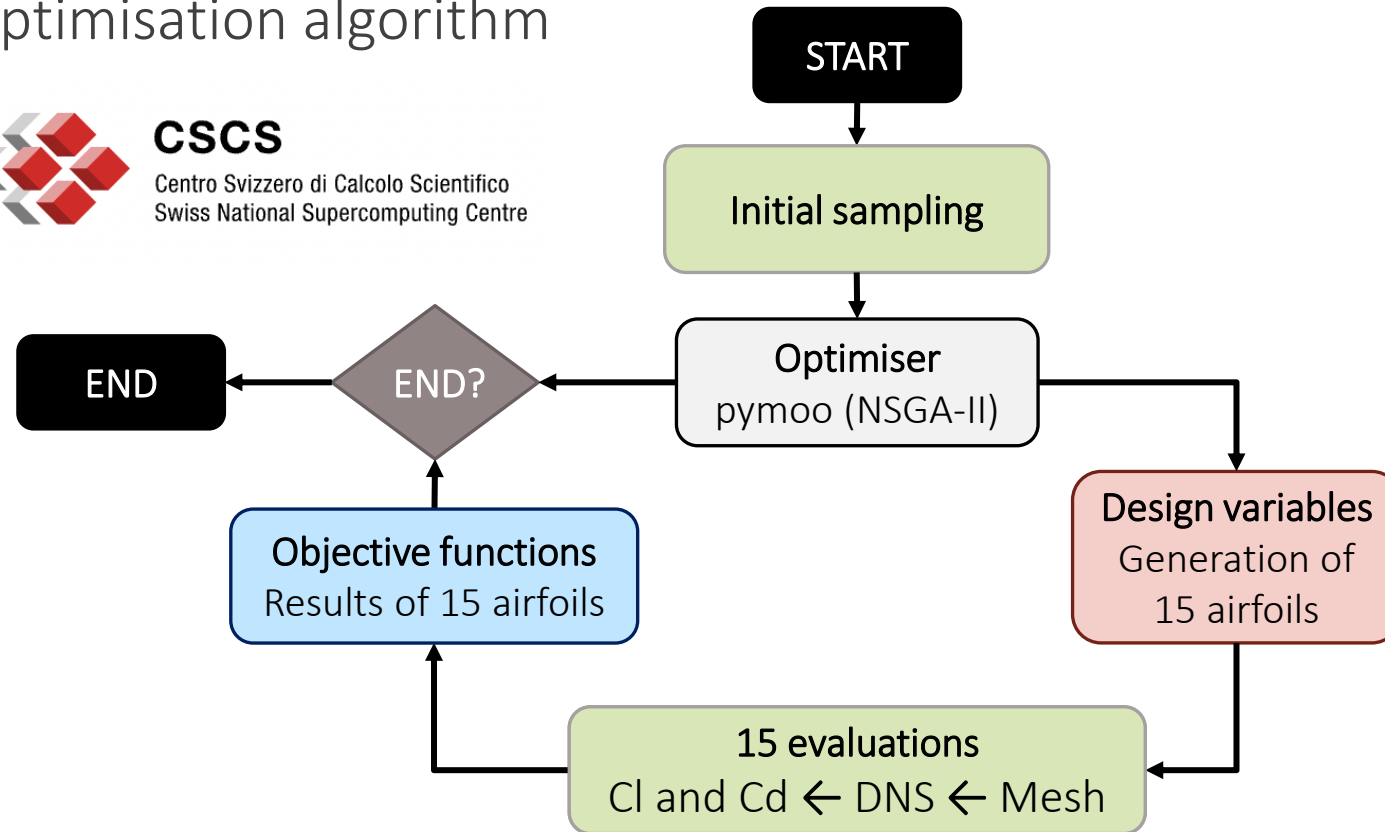
# Optimisation setup

## Optimisation algorithm



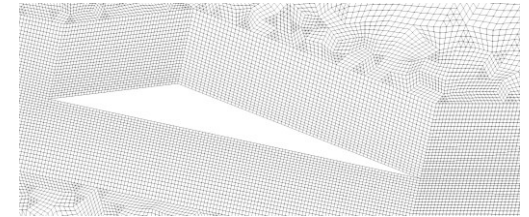
**CSCS**

Centro Svizzero di Calcolo Scientifico  
Swiss National Supercomputing Centre

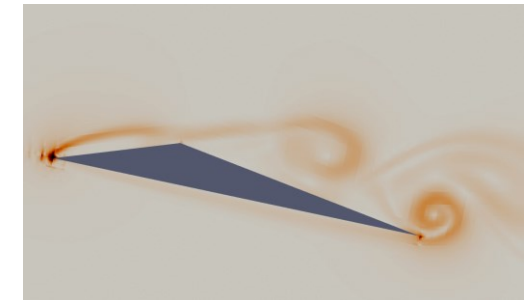


## Evaluation

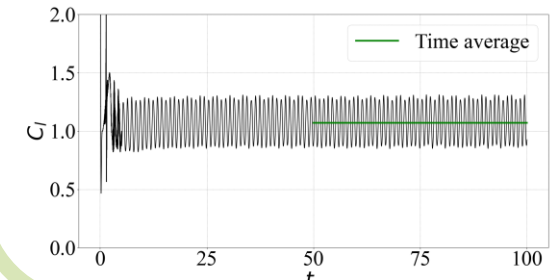
Mesh adaptation with Gmsh



3D DNS with PyFR



Aerodynamic forces

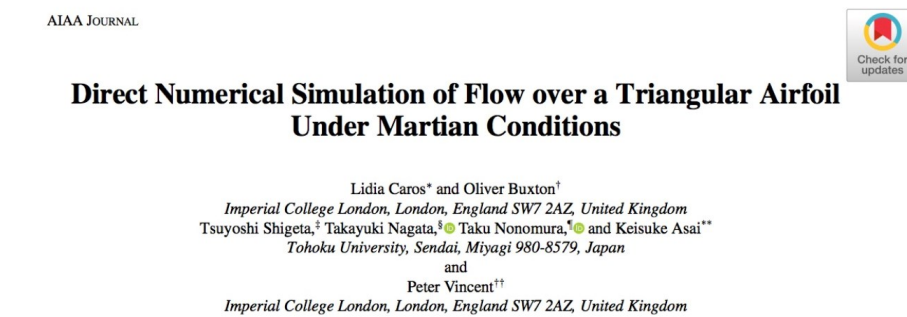


# Outline

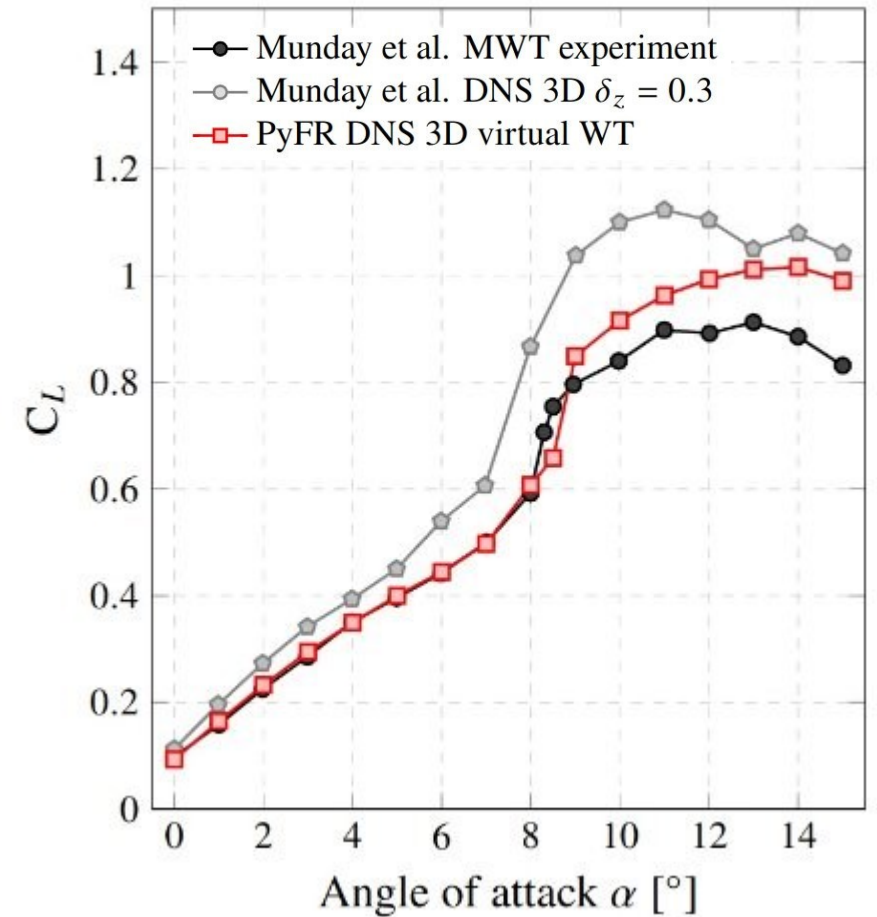
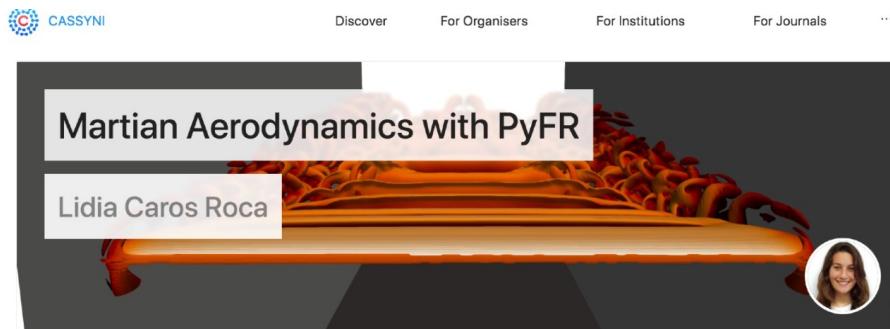
- Introduction
- Optimisation setup
- **Optimisation results**
- Effects of free-stream eddies
- Summary and future work

# Validation

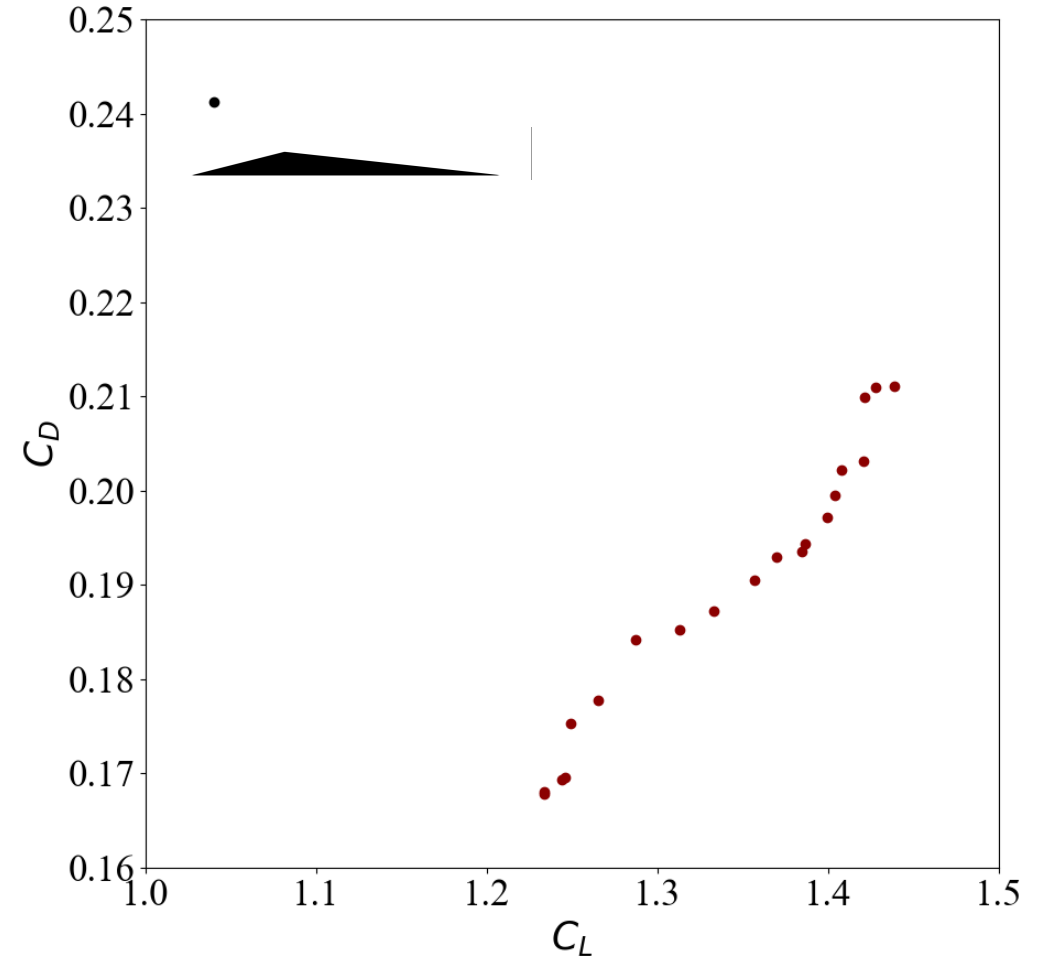
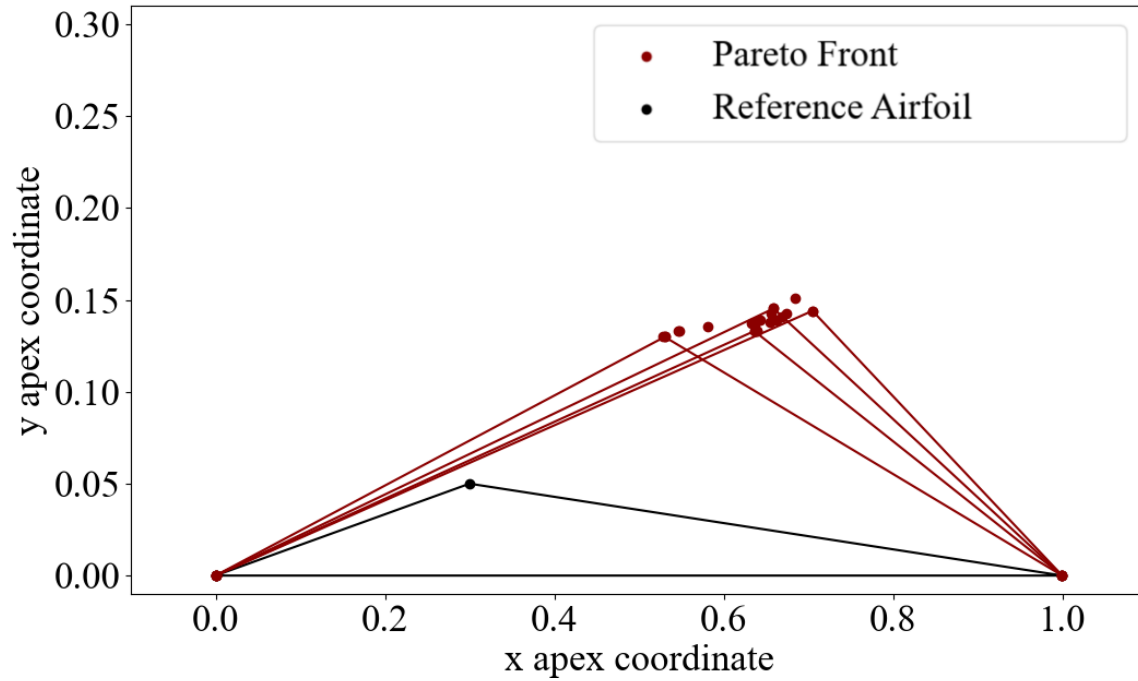
Paper: L. Caros et al. AIAA Journal 2022 10.2514/1.J061454



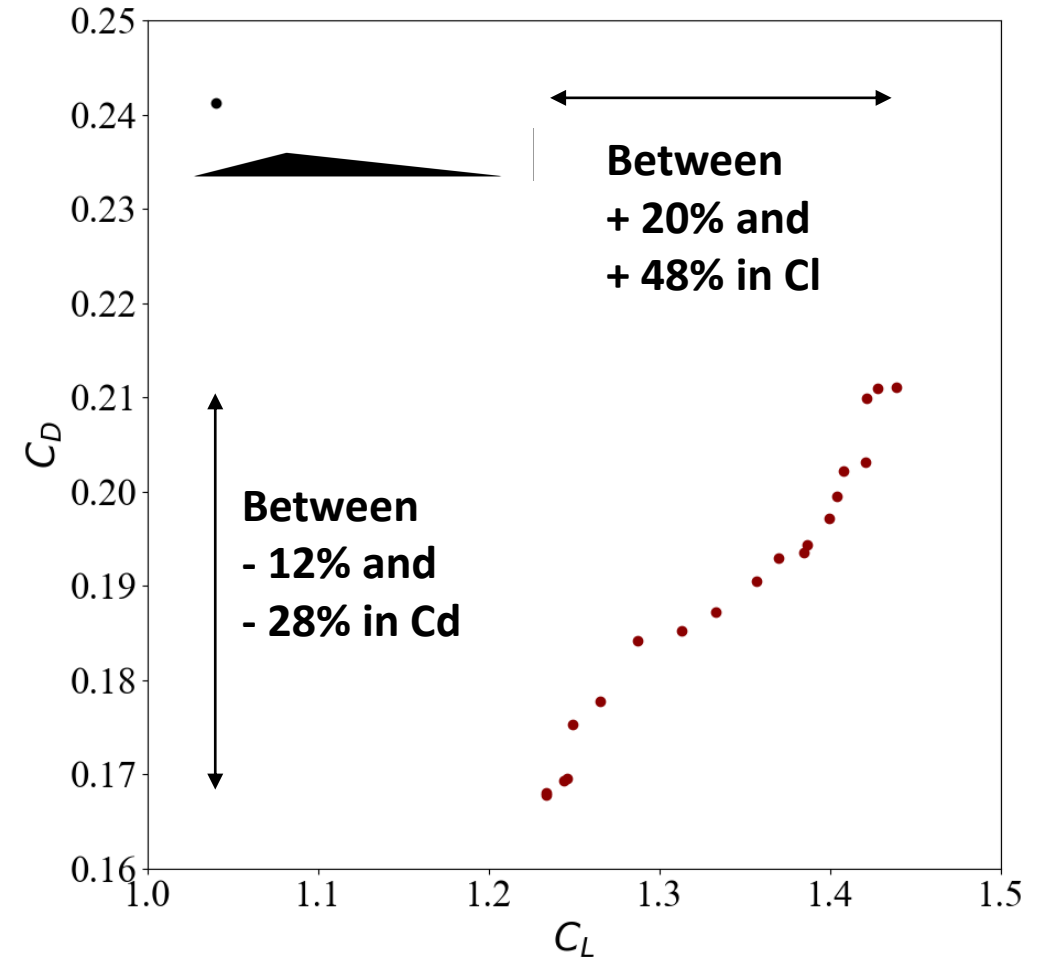
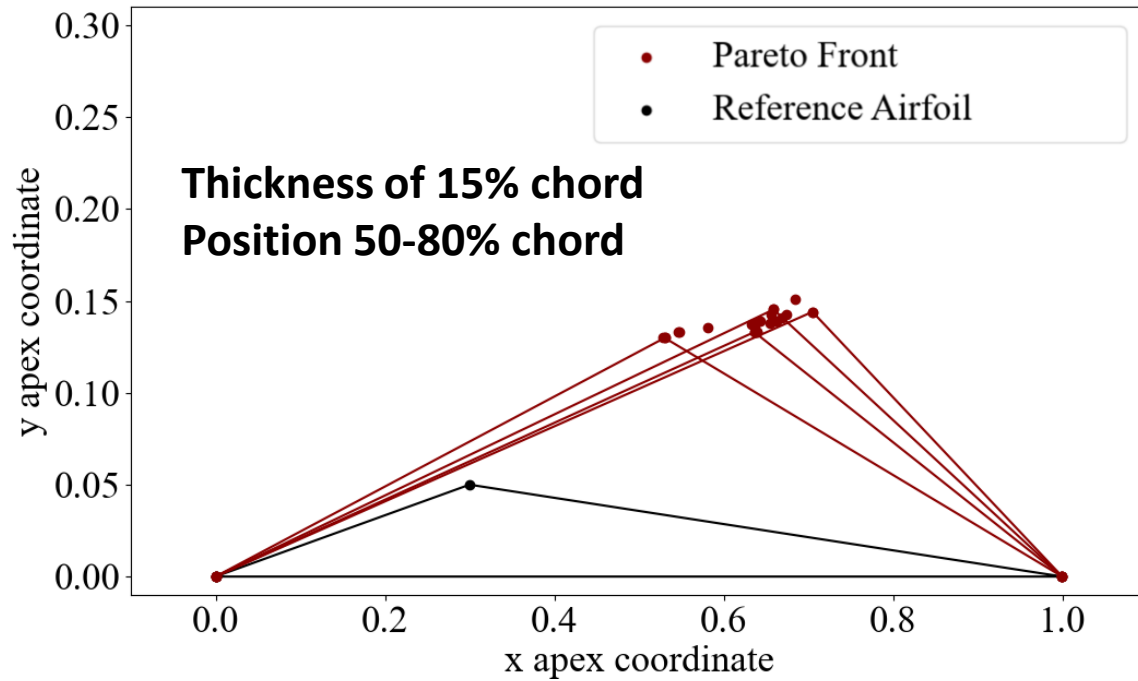
Seminar: L. Caros. Cassini 2021 10.52843/47ly7q



# Optimisation Results

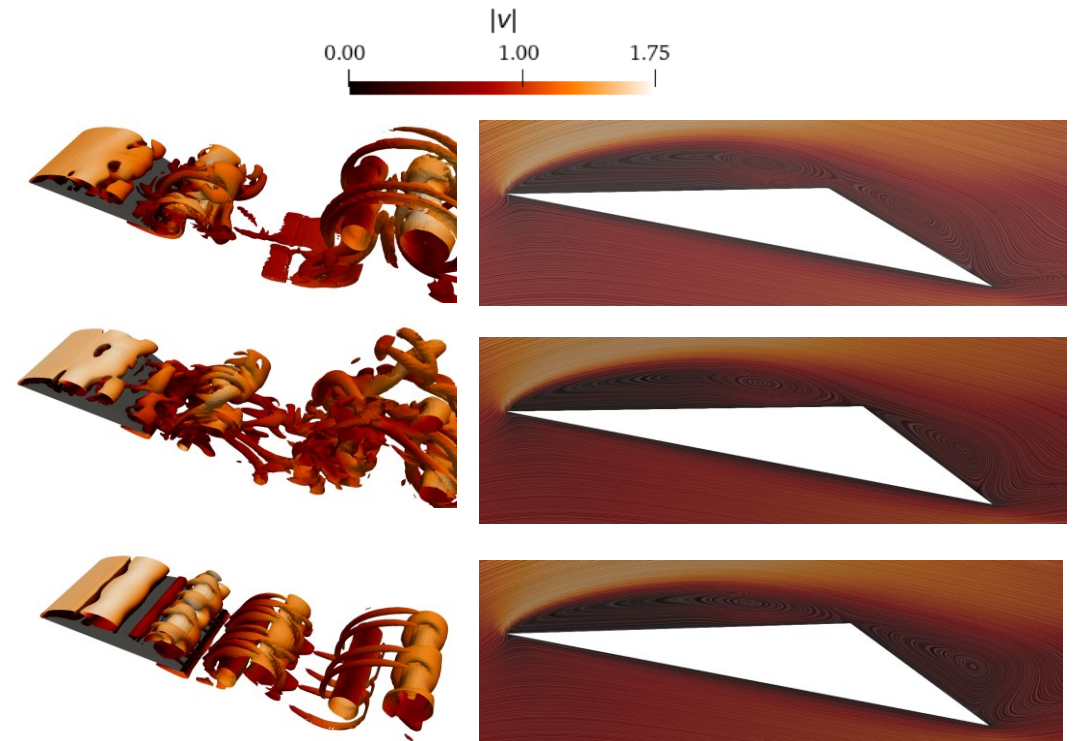
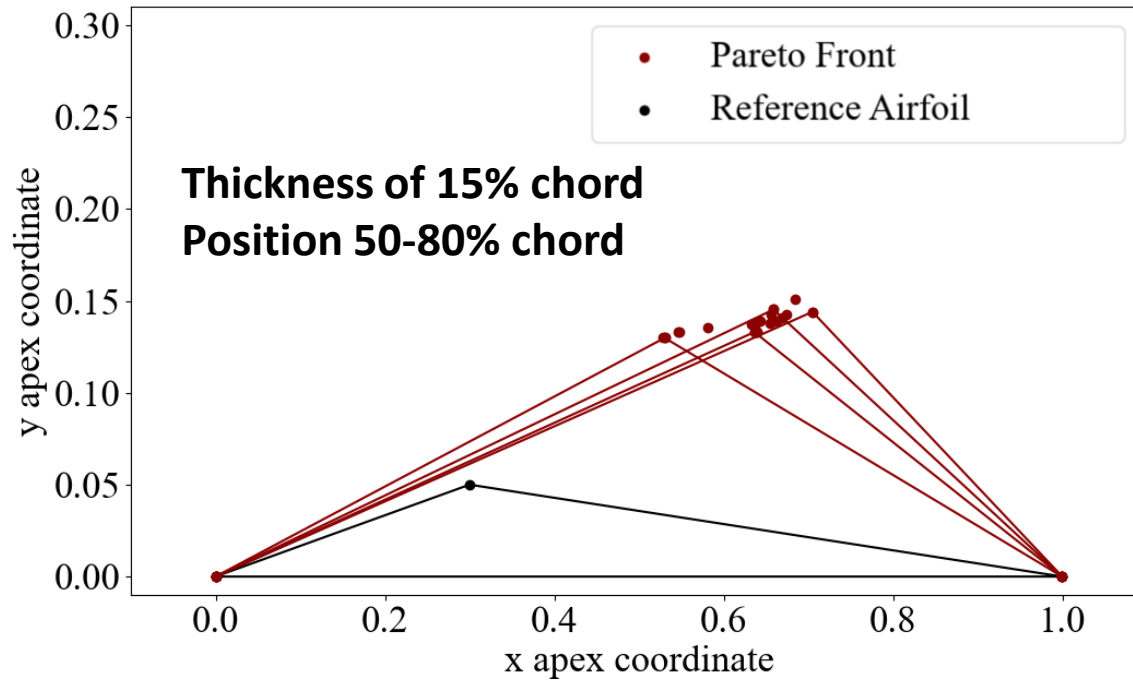


# Optimisation Results



# Optimisation Results

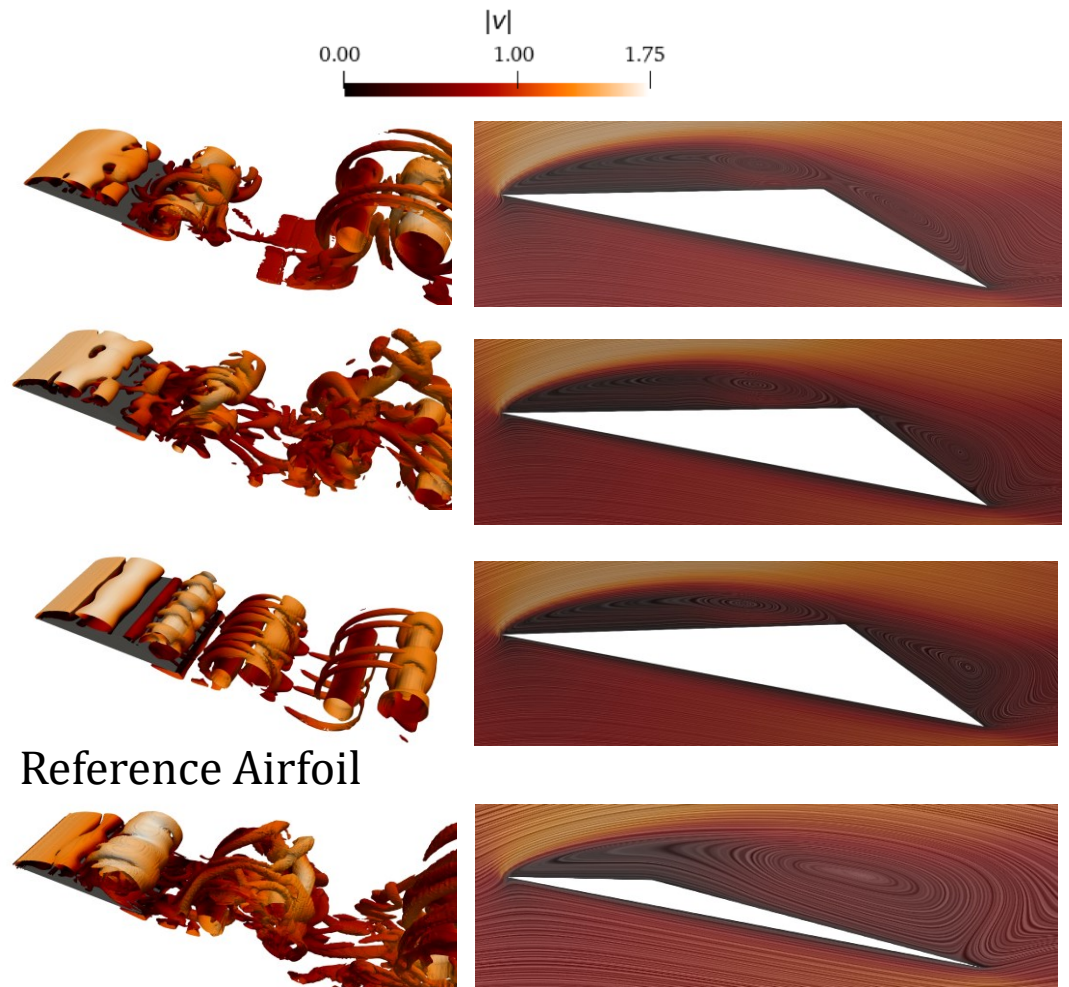
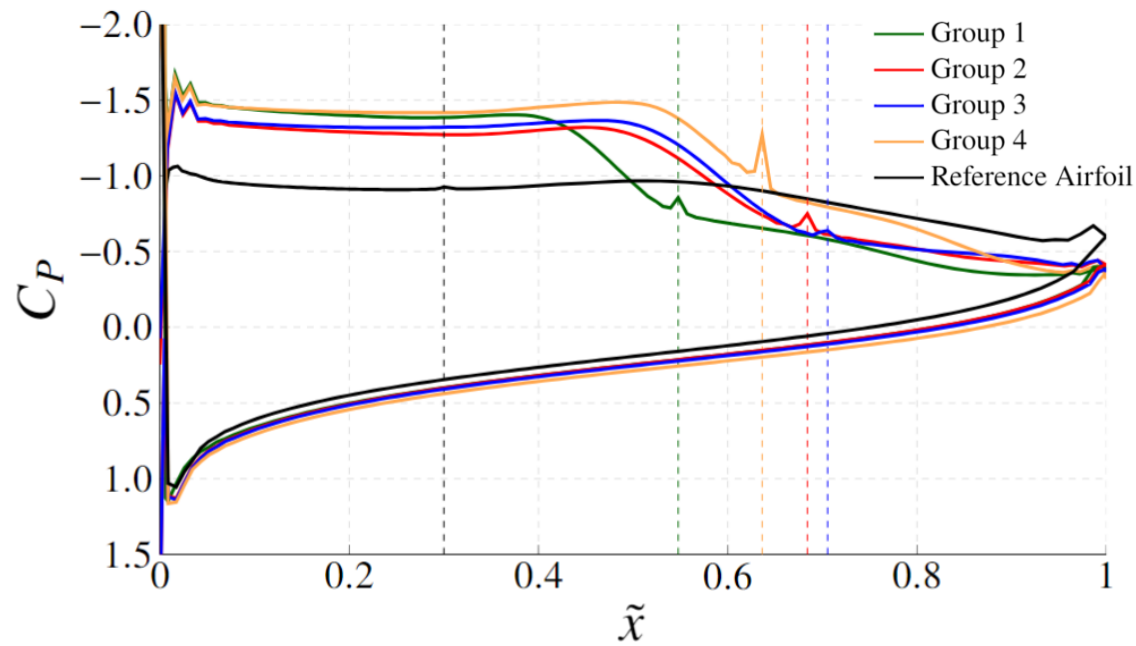
All exploit vortex roll-up. First suction surface almost parallel to the flow.





# Optimisation Results

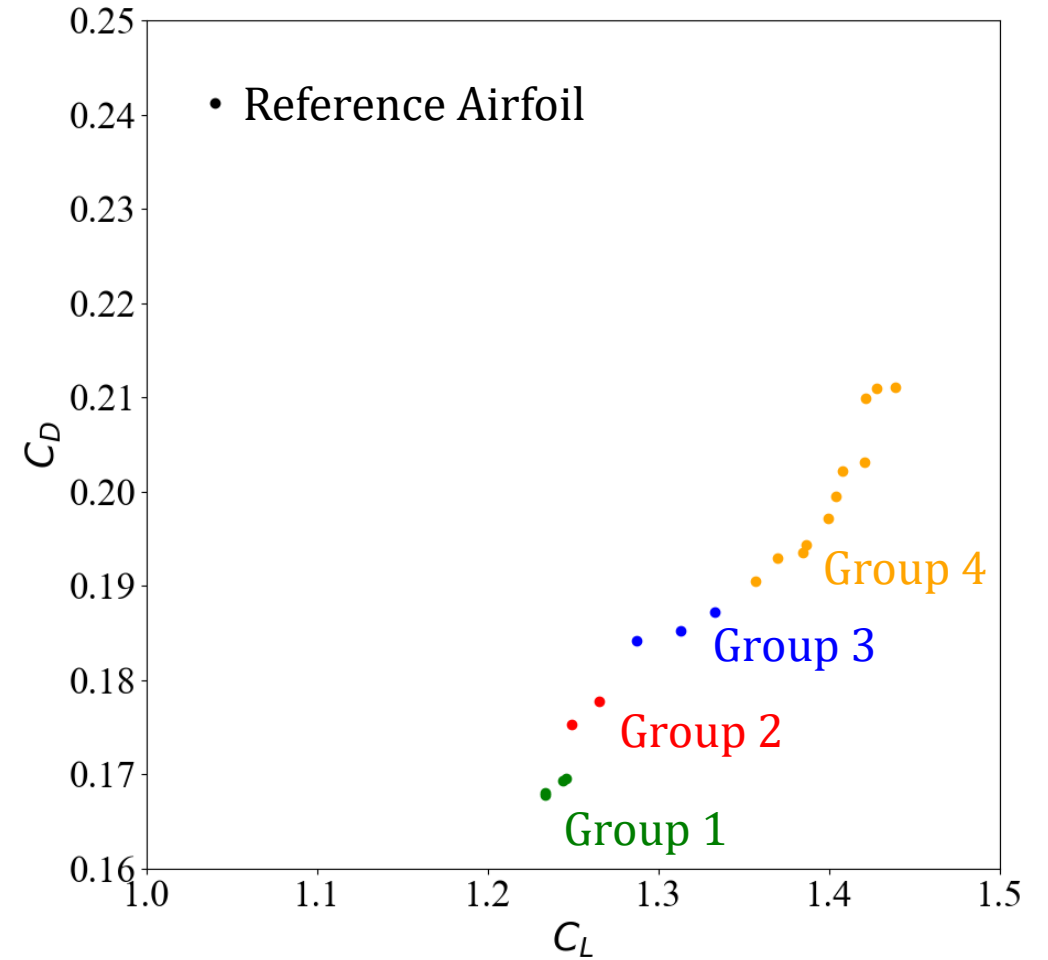
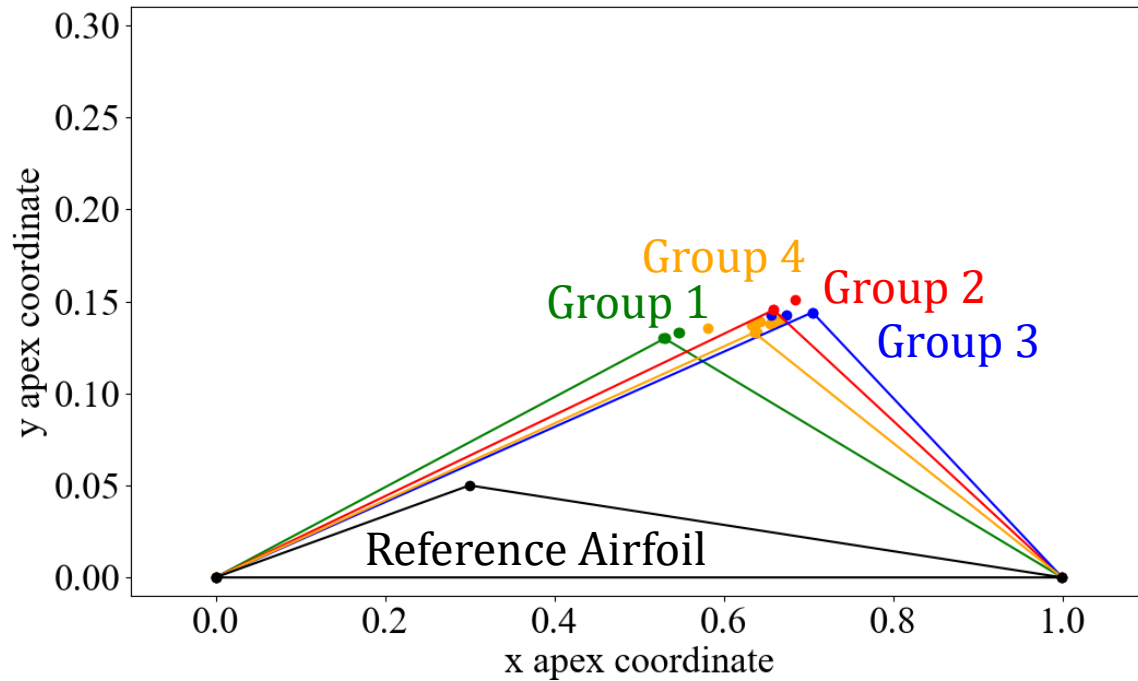
All exploit vortex roll-up. First suction surface almost parallel to the flow.



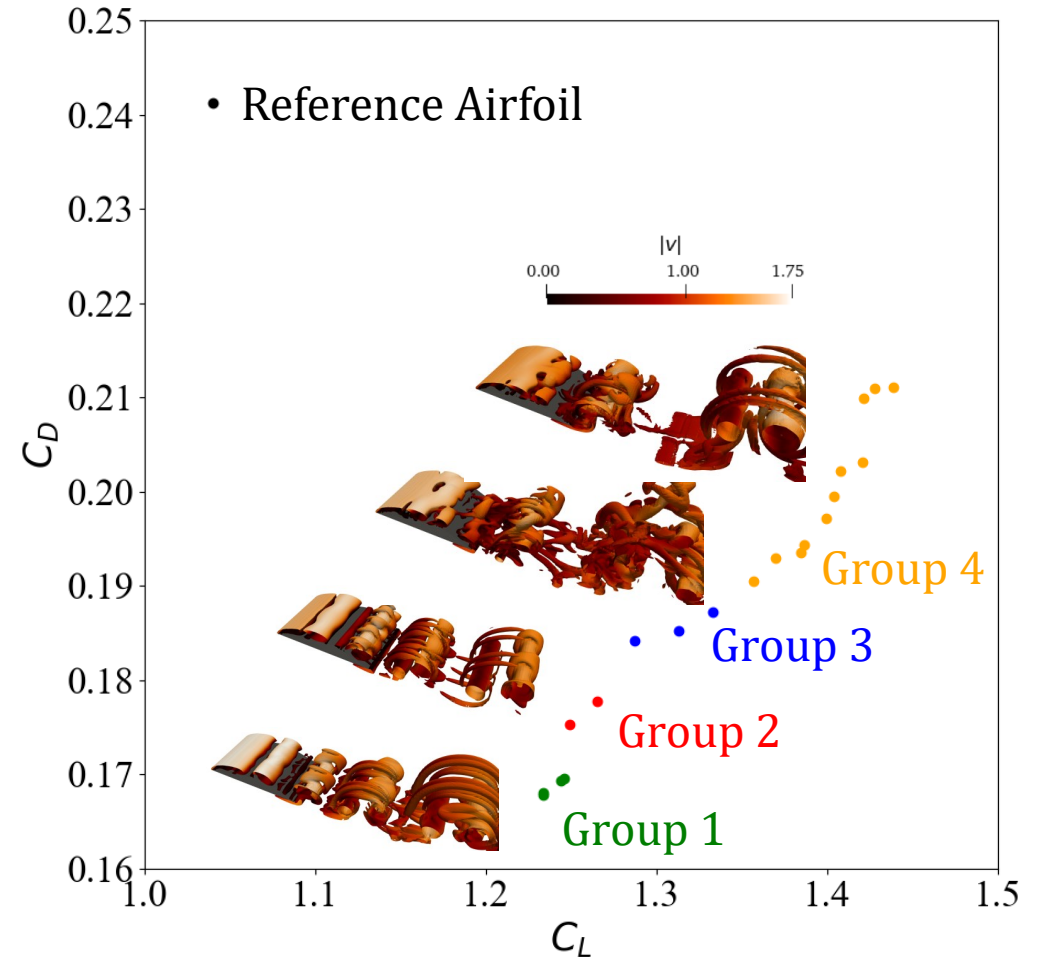
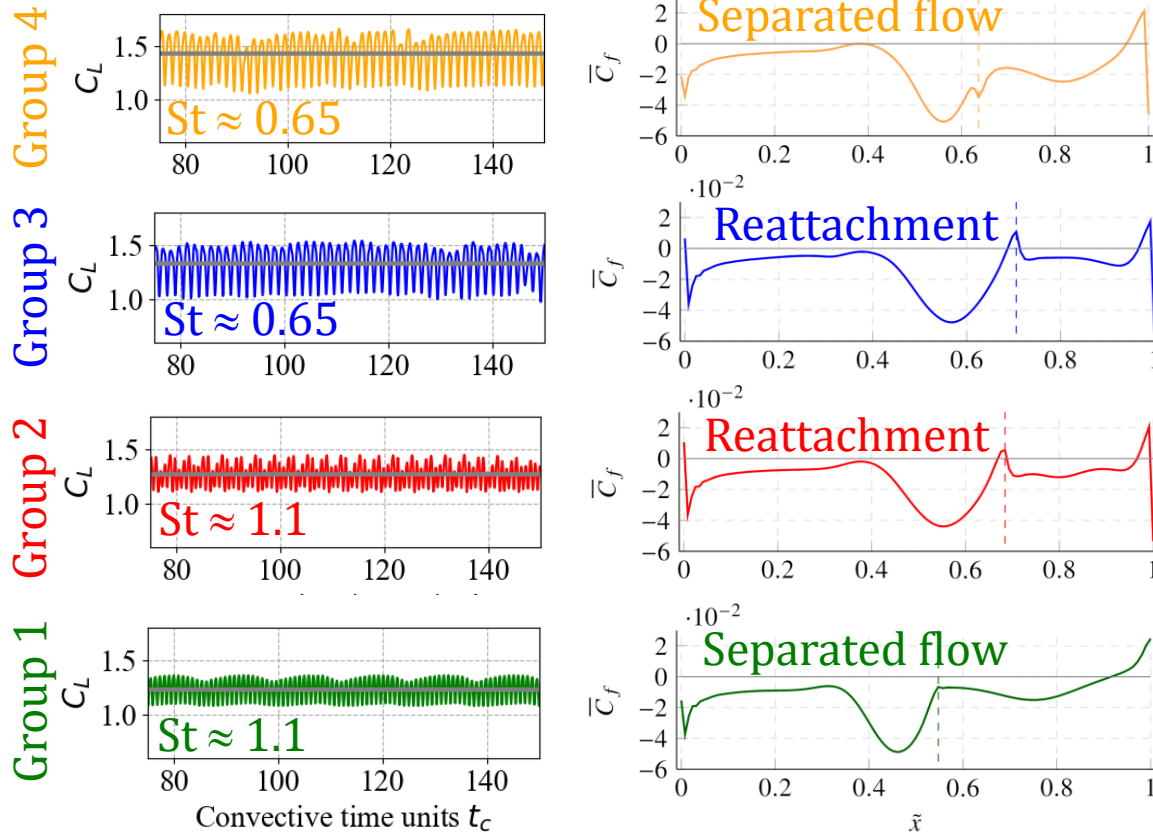
Reference Airfoil

# Optimisation Results

Identified four groups based on flow characteristics



# Optimisation Results



# Optimisation Results

Paper: L. Caros et al. AIAA Journal 2023 10.2514/1.J063164

AIAA JOURNAL  
Vol. 61, No. 11, November 2023

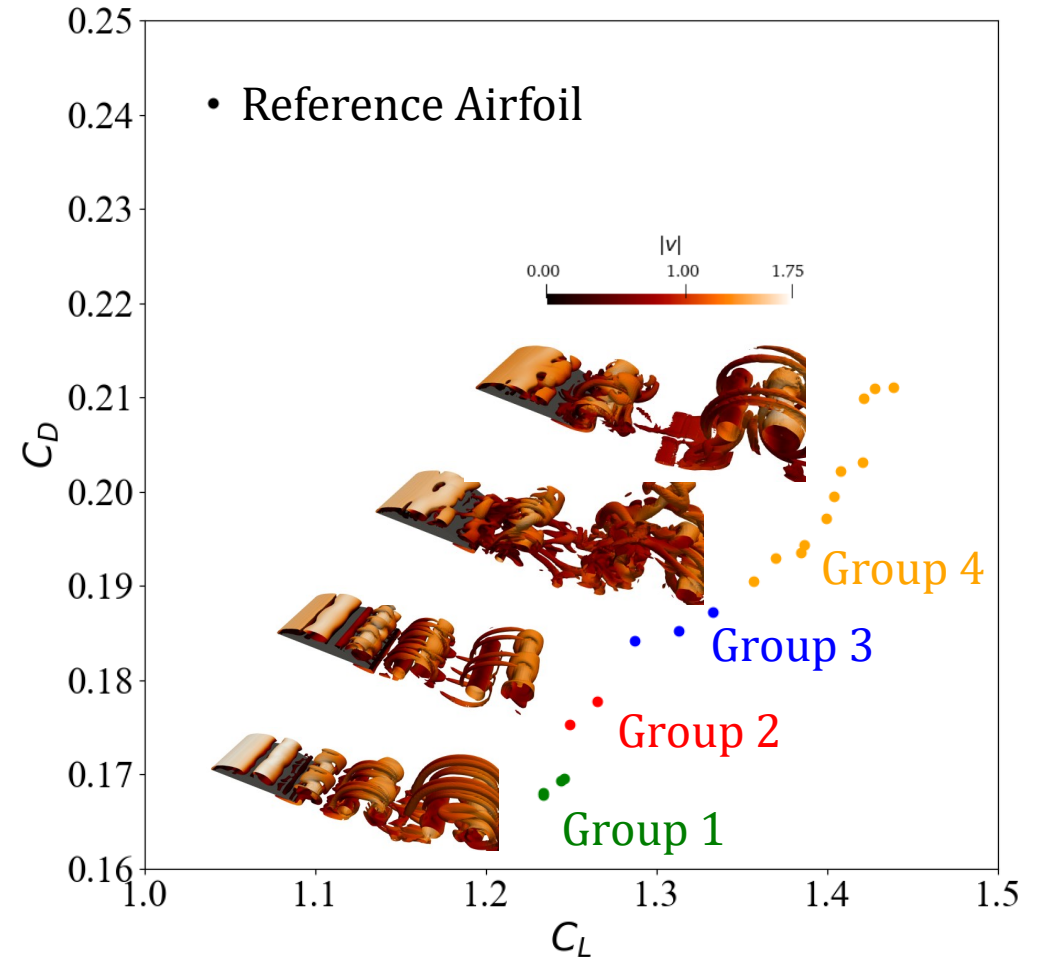


## Optimization of Triangular Airfoils for Martian Helicopters Using Direct Numerical Simulations

Lidia Caros,<sup>\*</sup> Oliver Buxton,<sup>†</sup> and Peter Vincent<sup>‡</sup>  
Imperial College London, London, England SW7 2AZ, United Kingdom  
<https://doi.org/10.2514/1.J063164>

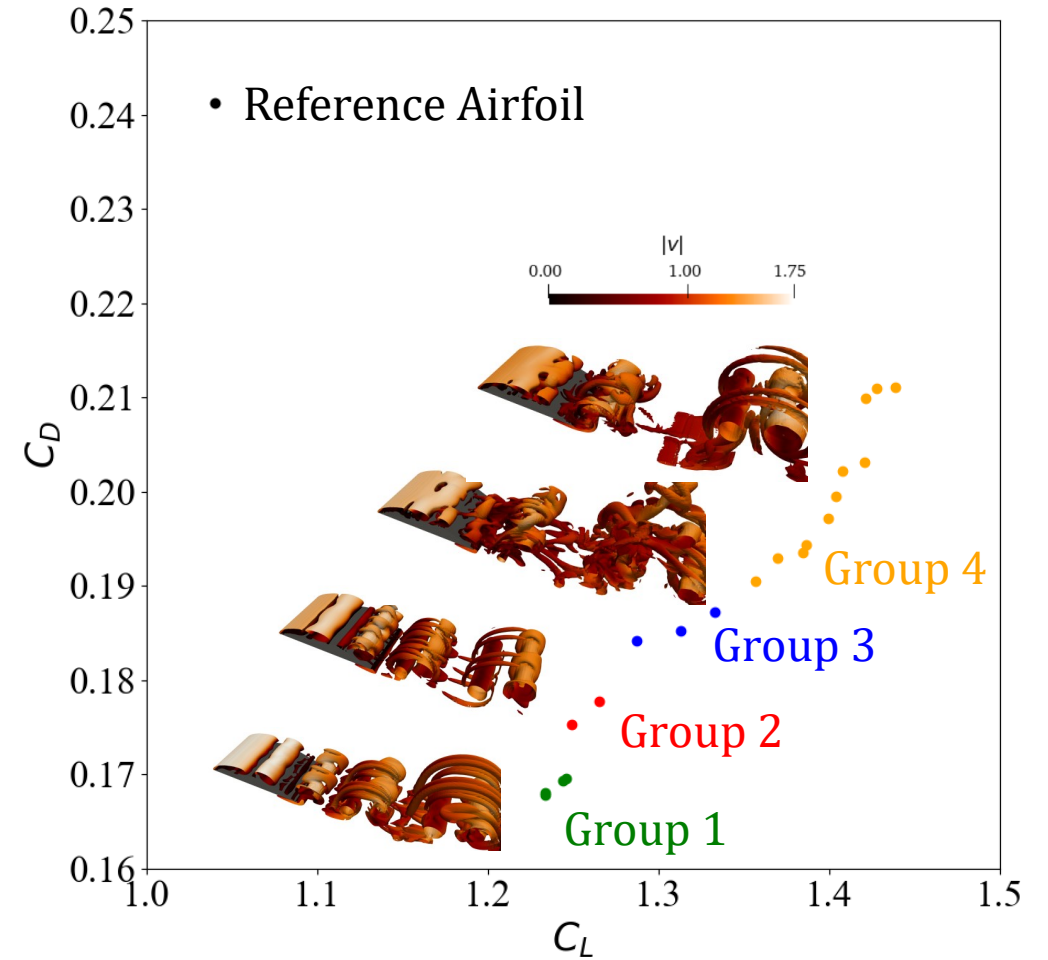
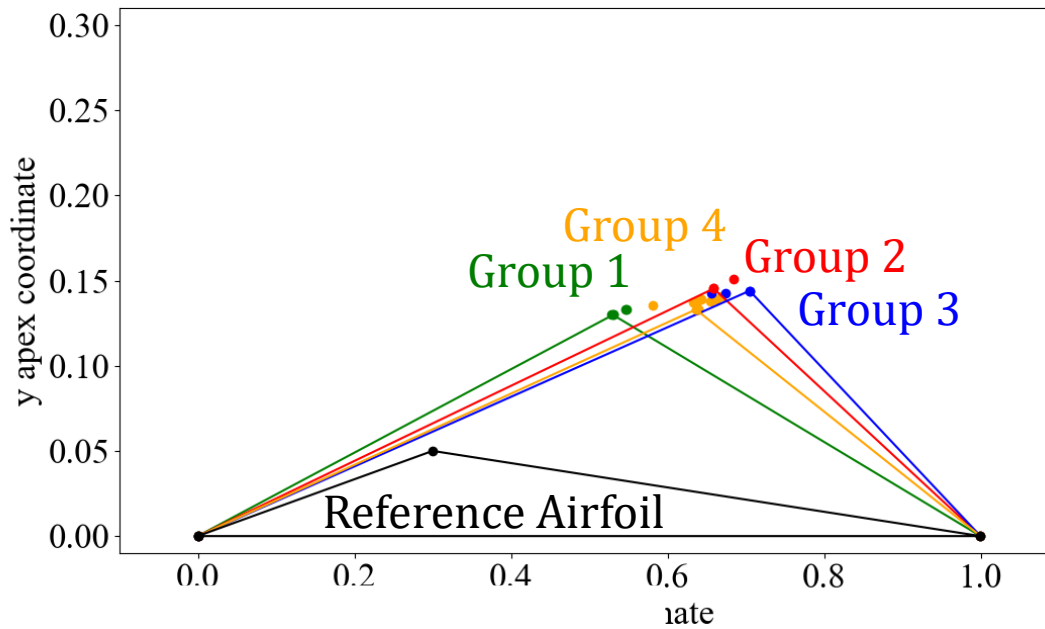
Mars has a lower atmospheric density than Earth, and the speed of sound is lower due to its atmospheric composition and lower surface temperature. Consequently, Martian rotor blades operate in a low-Reynolds-number compressible regime that is atypical for terrestrial helicopters. Nonconventional airfoils with sharp edges and flat surfaces have shown improved performance under such conditions, and second-order-accurate Reynolds-

Seminar: L. Caros. Cassyni 2023 10.52843/cassyni.6r5ry1



# Optimisation Results

How sensitive will these airfoils be to perturbations in the flow?



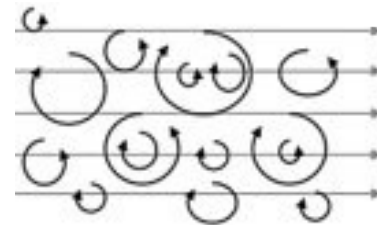
# Outline

- Introduction
- Optimisation setup
- Optimisation results
- **Effects of free-stream eddies**
- Summary and future work

## Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

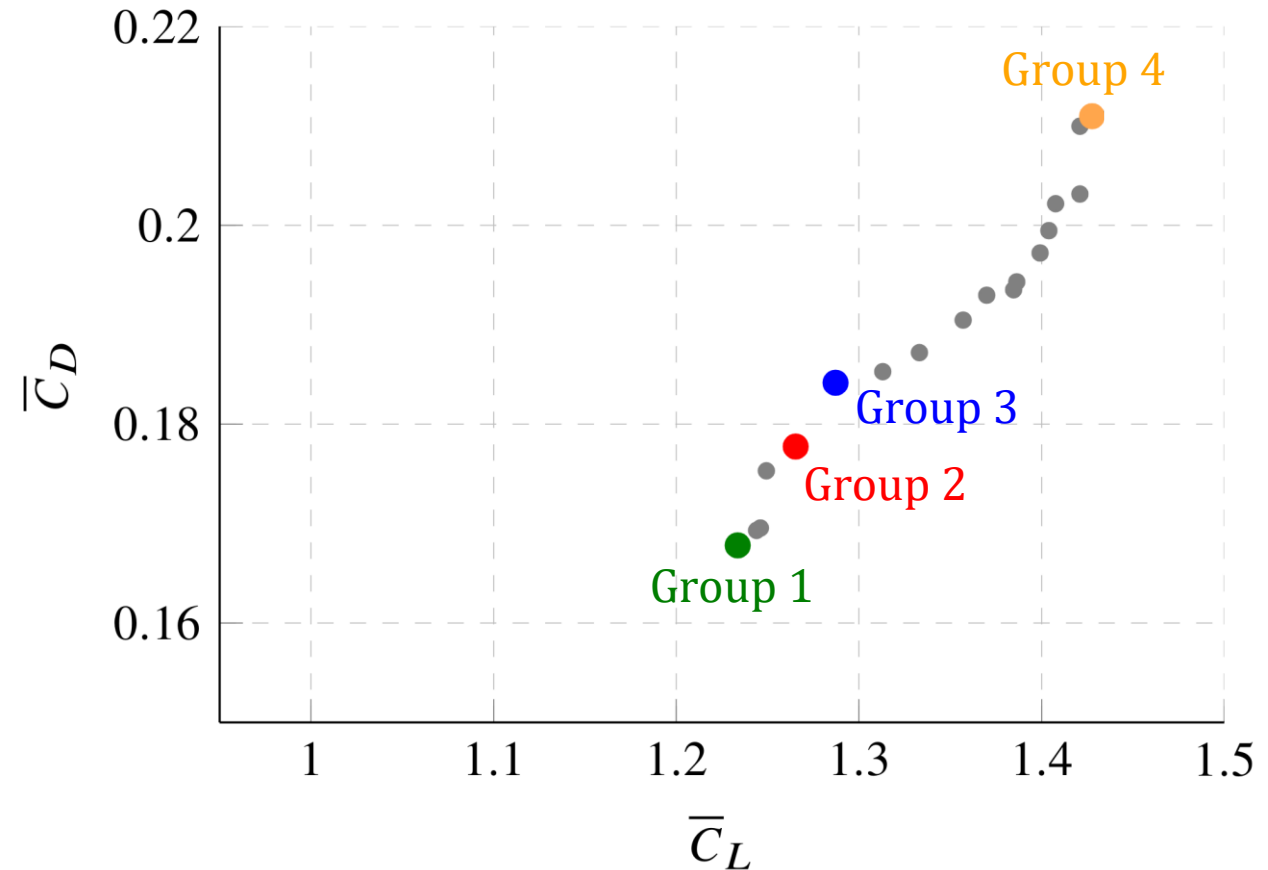
- Target turbulence intensities  
 $TI=1\%$  and  $TI=0.5\%$
- Target integral lengthscales  
 $l_s=0.1c$  and  $l_s=0.05c$



## Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
Is=0.1c and Is=0.05c

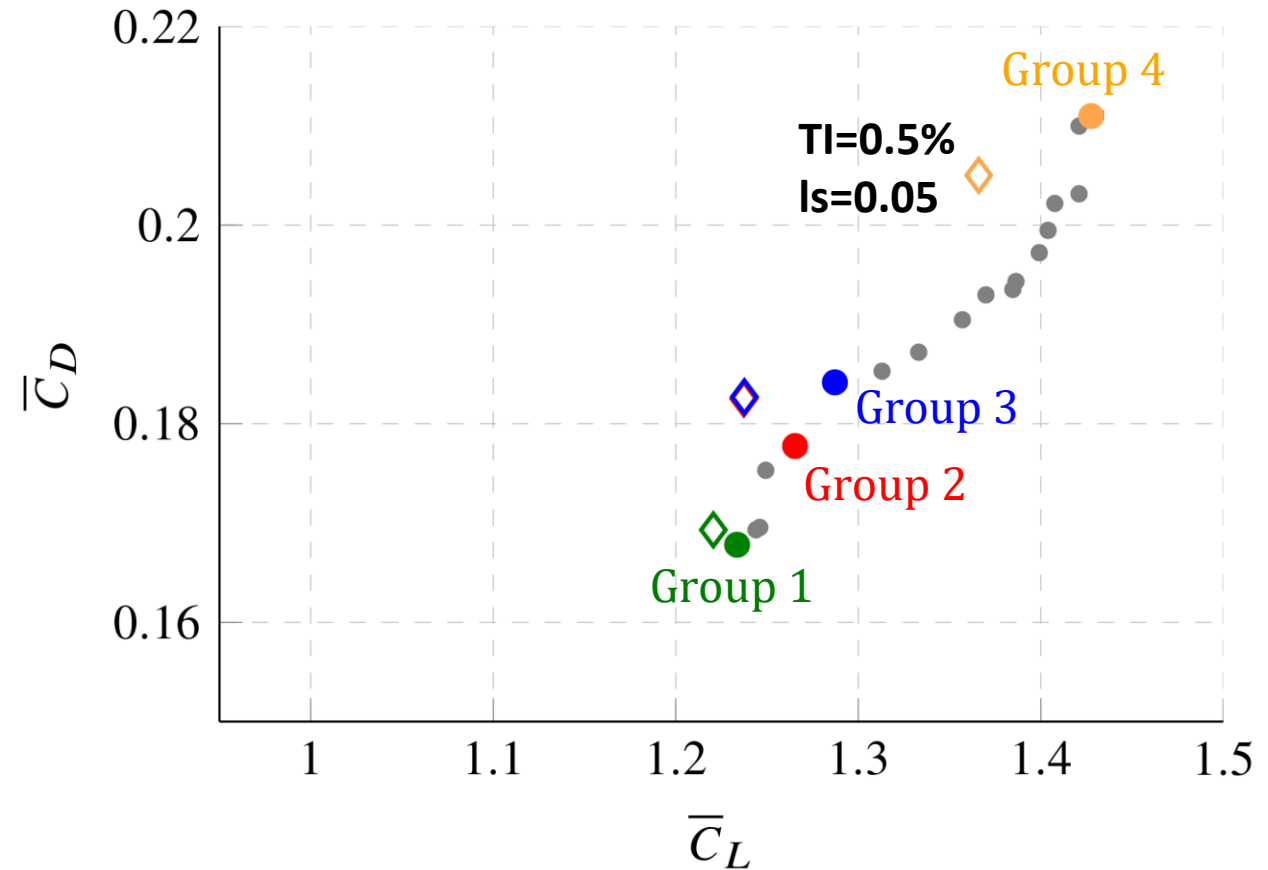




## Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

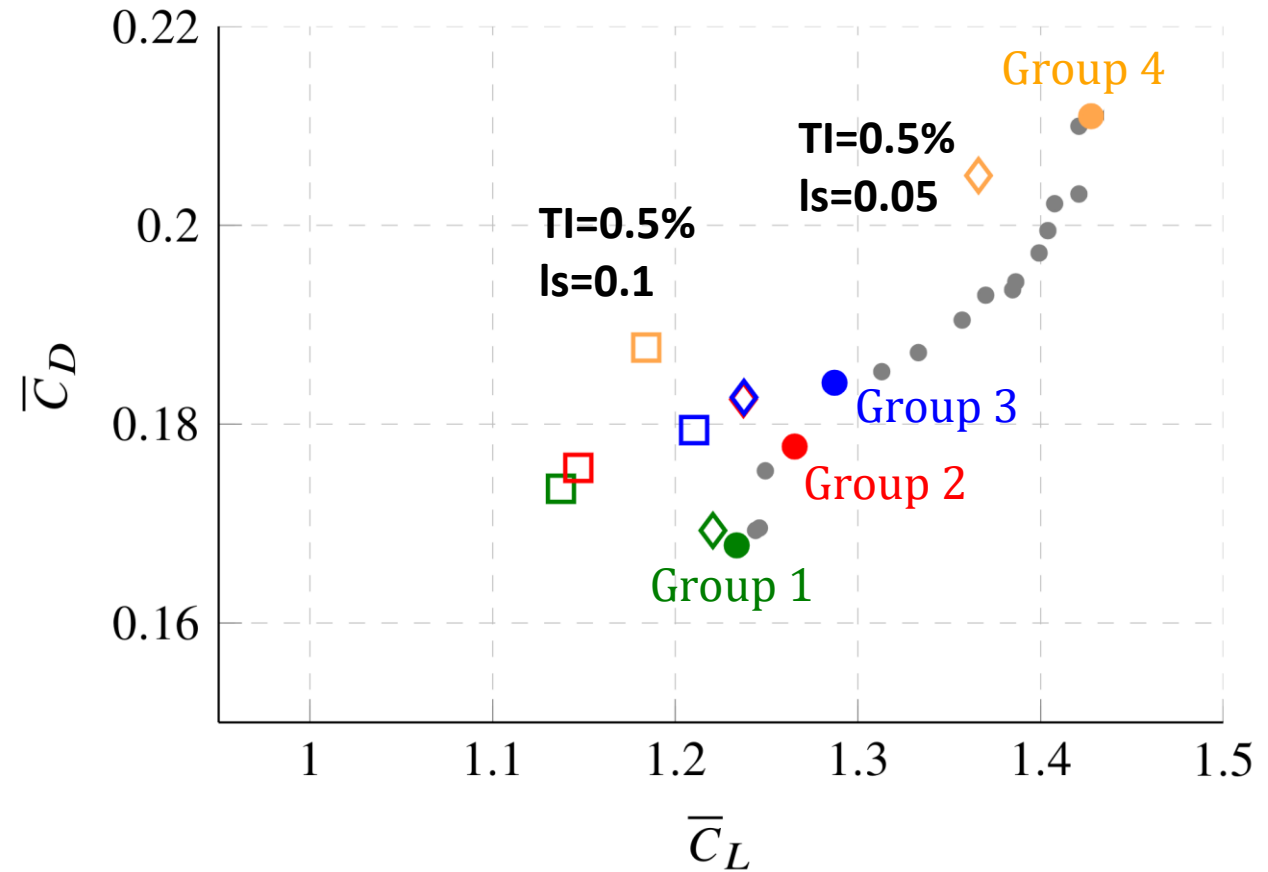
- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
Is=0.1c and Is=0.05c



## Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

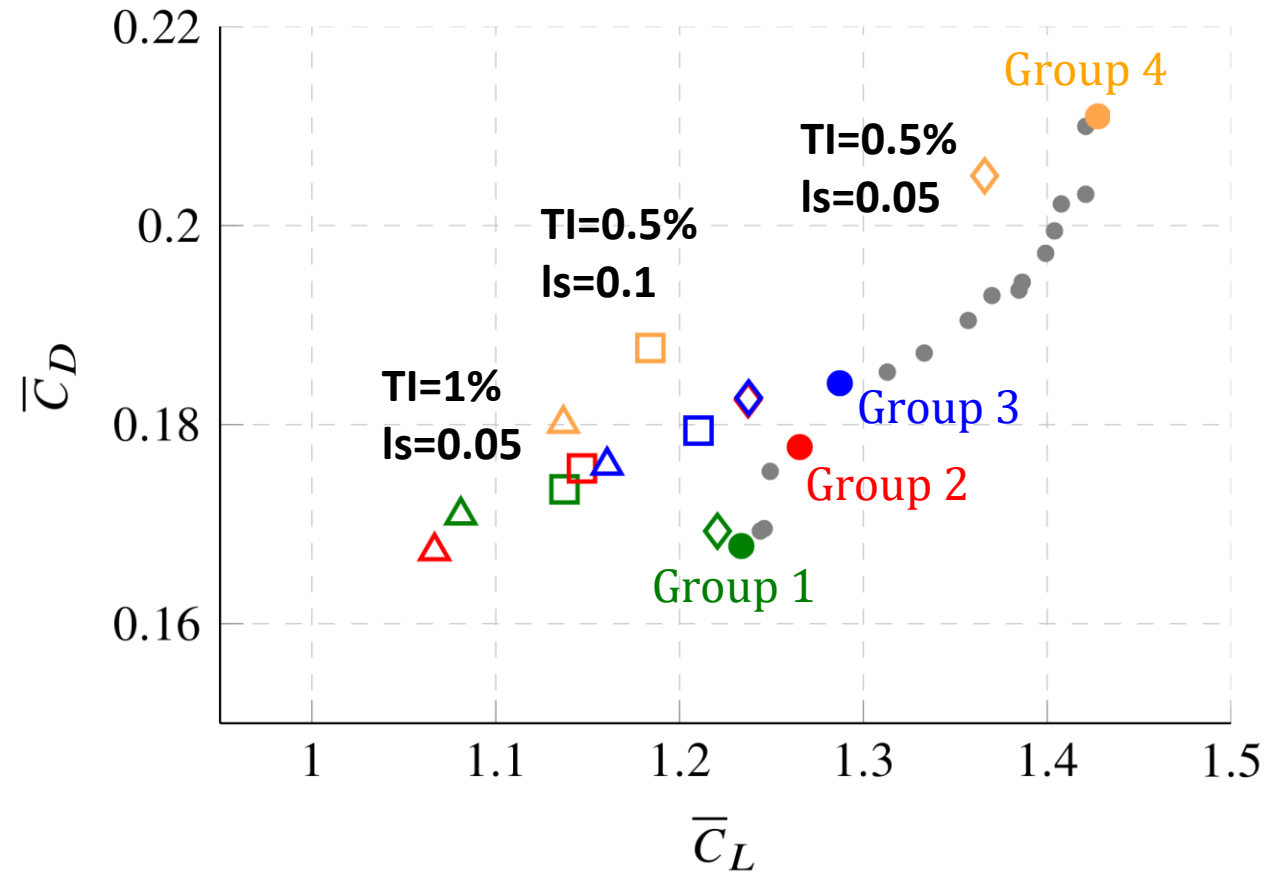
- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
Is=0.1c and Is=0.05c



# Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

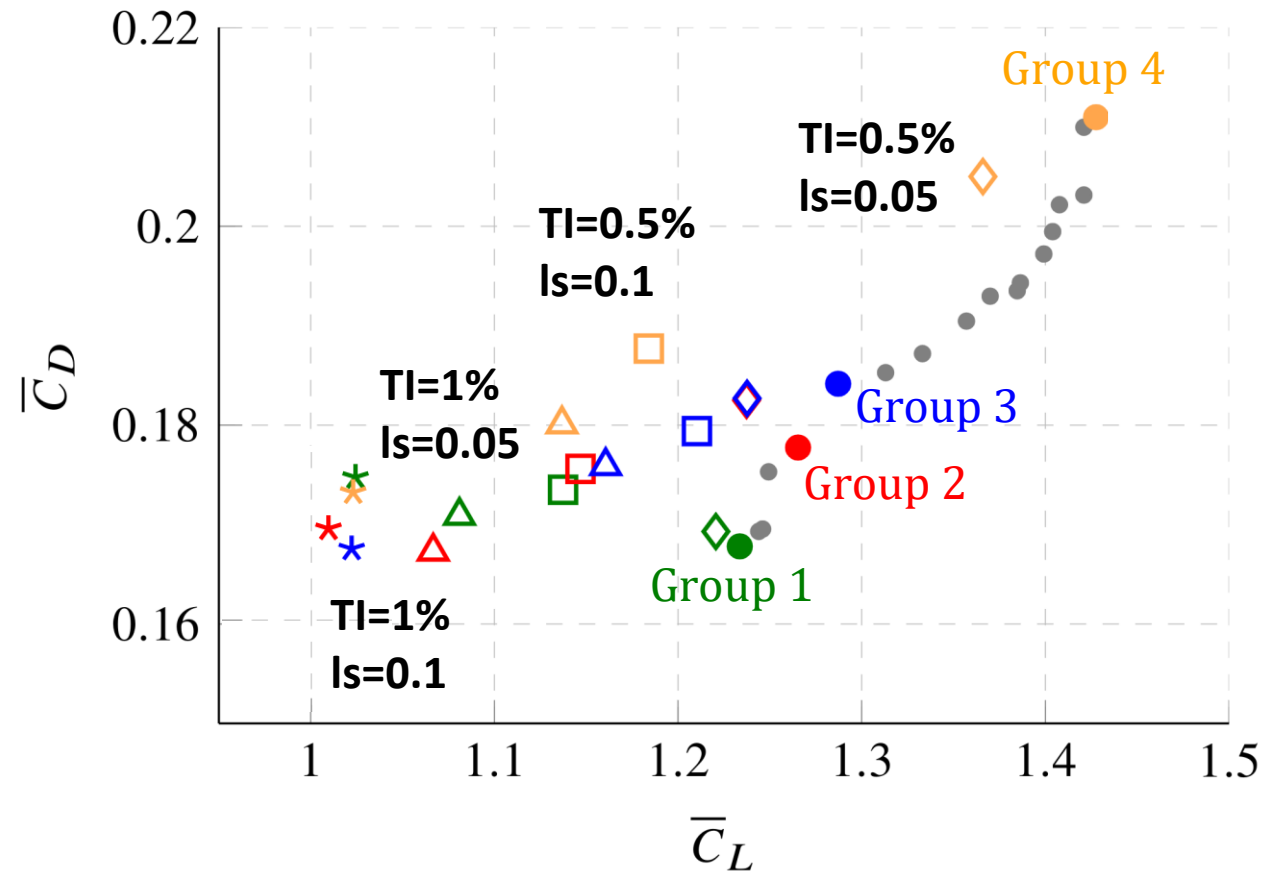
- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
Is=0.1c and Is=0.05c



## Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

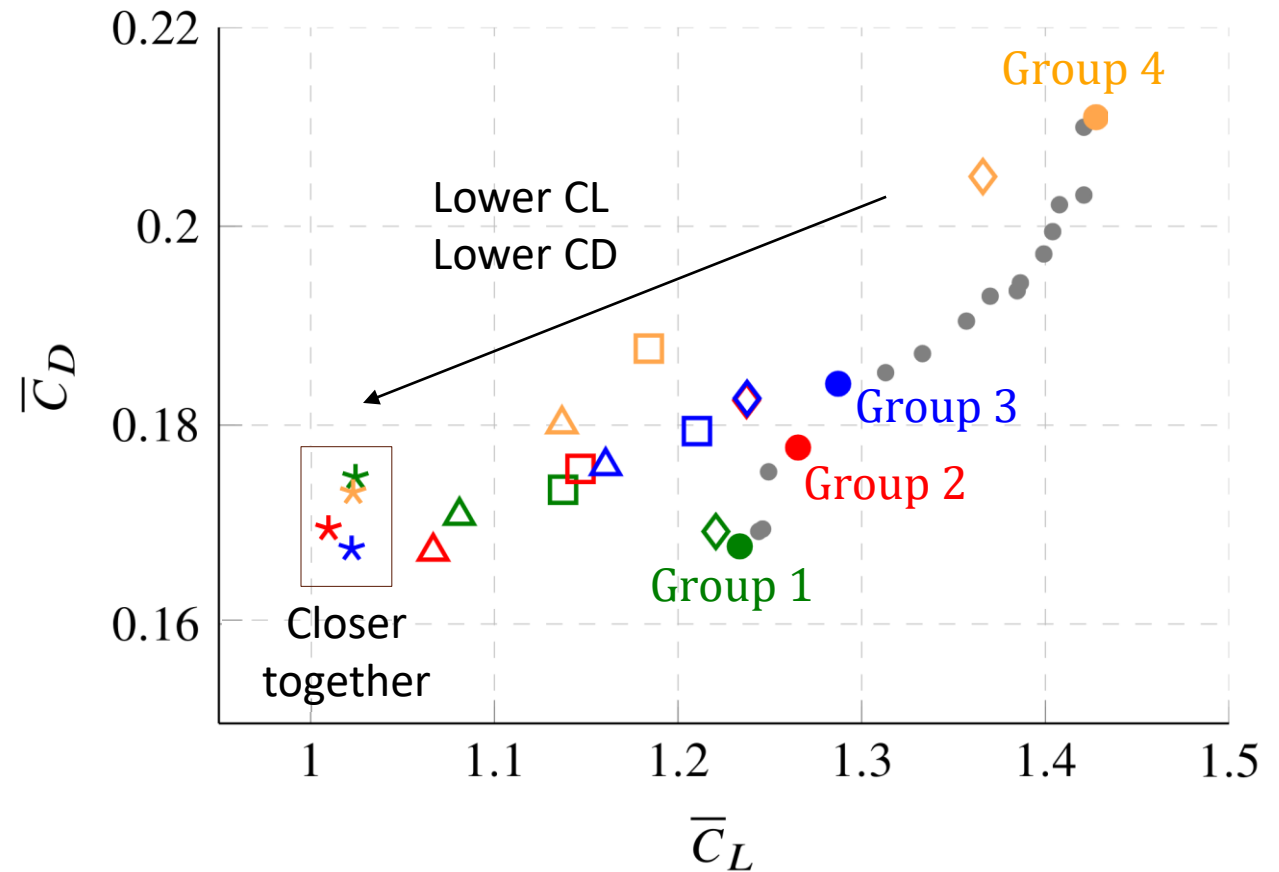
- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
Is=0.1c and Is=0.05c



# Effects of free-stream eddies on optimised airfoils

Injection of eddies with the Synthetic Eddy Method implemented in PyFR

- Target turbulence intensities  
TI=1% and TI=0.5%
- Target integral lengthscales  
ls=0.1c and ls=0.05c

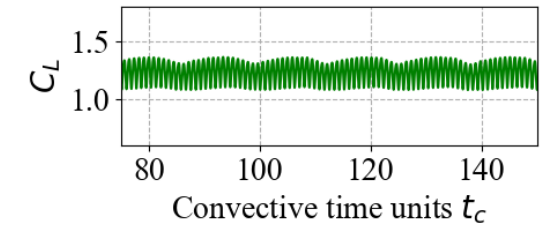
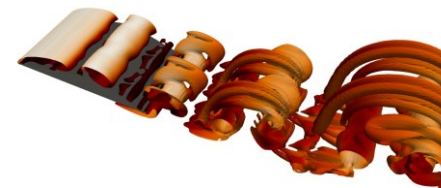


# Effects of free-stream eddies on optimised airfoils

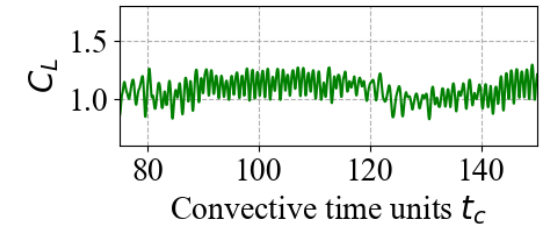
- Free-stream eddies tend to break the periodicity of the flow due to the breakdown of the coherent vortices
- The higher the TI and  $I_s$ , the stronger the effect

Group 1

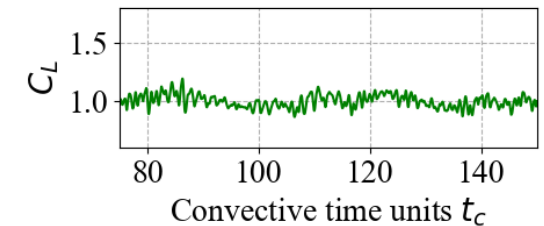
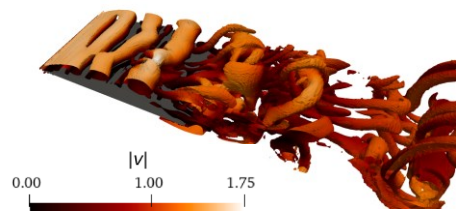
Uniform free-stream



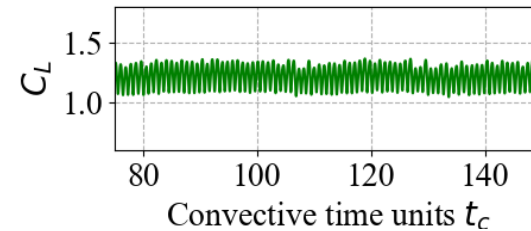
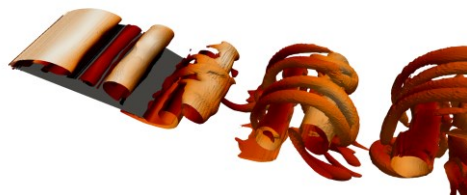
TI=0.5%  $I_s=0.1$



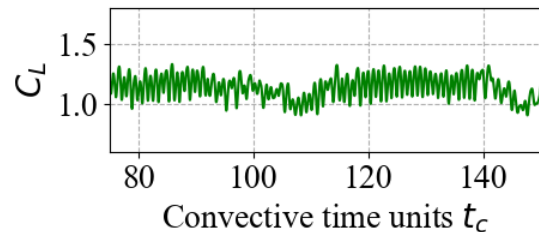
TI=1%  $I_s=0.1$



TI=0.5%  $I_s=0.05$



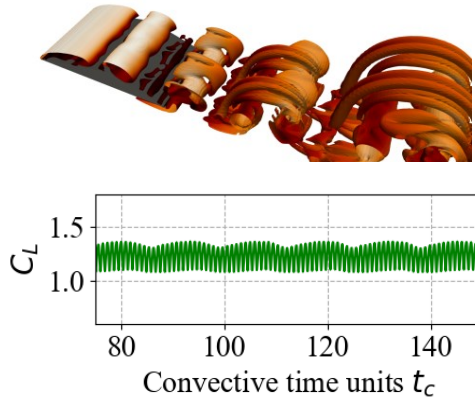
TI=1%  $I_s=0.05$



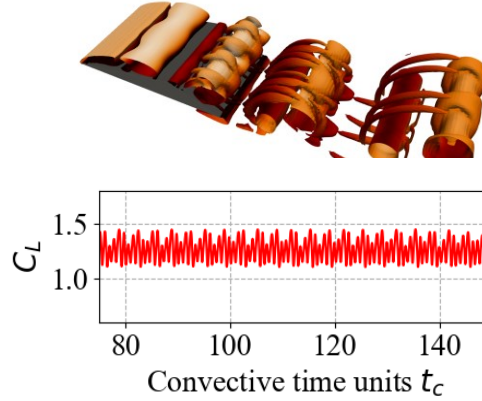
# Effects of free-stream eddies on optimised airfoils

Uniform free-stream

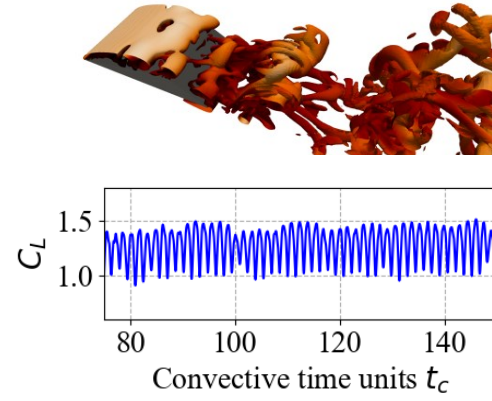
Group 1



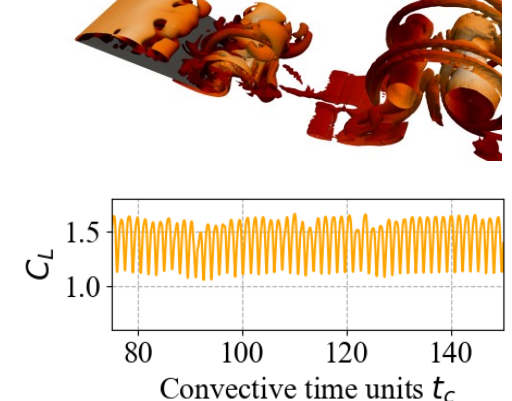
Group 2



Group 3

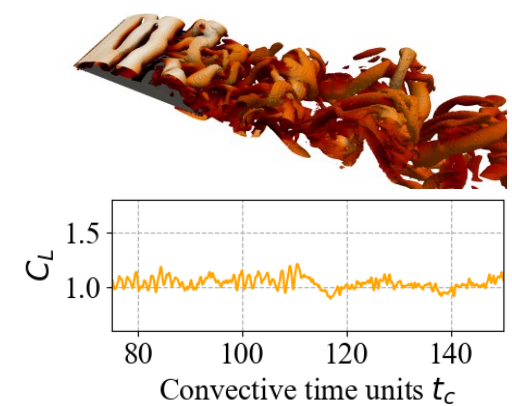
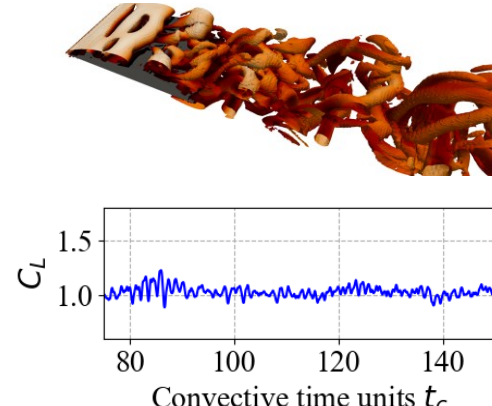
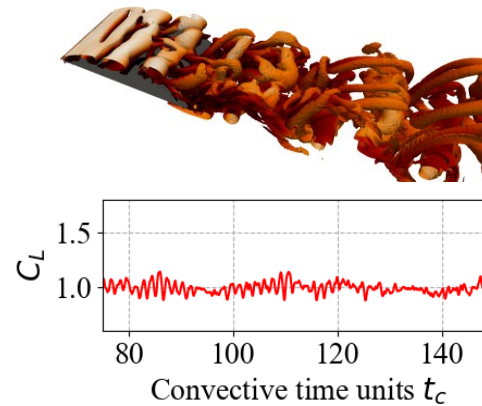
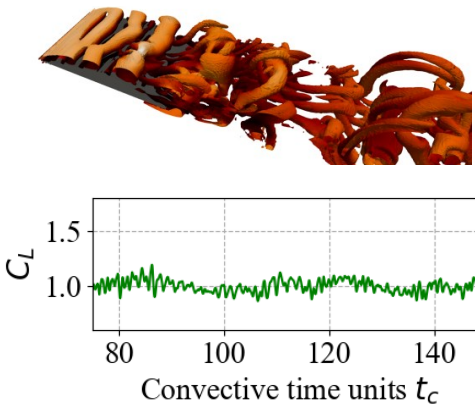


Group 4



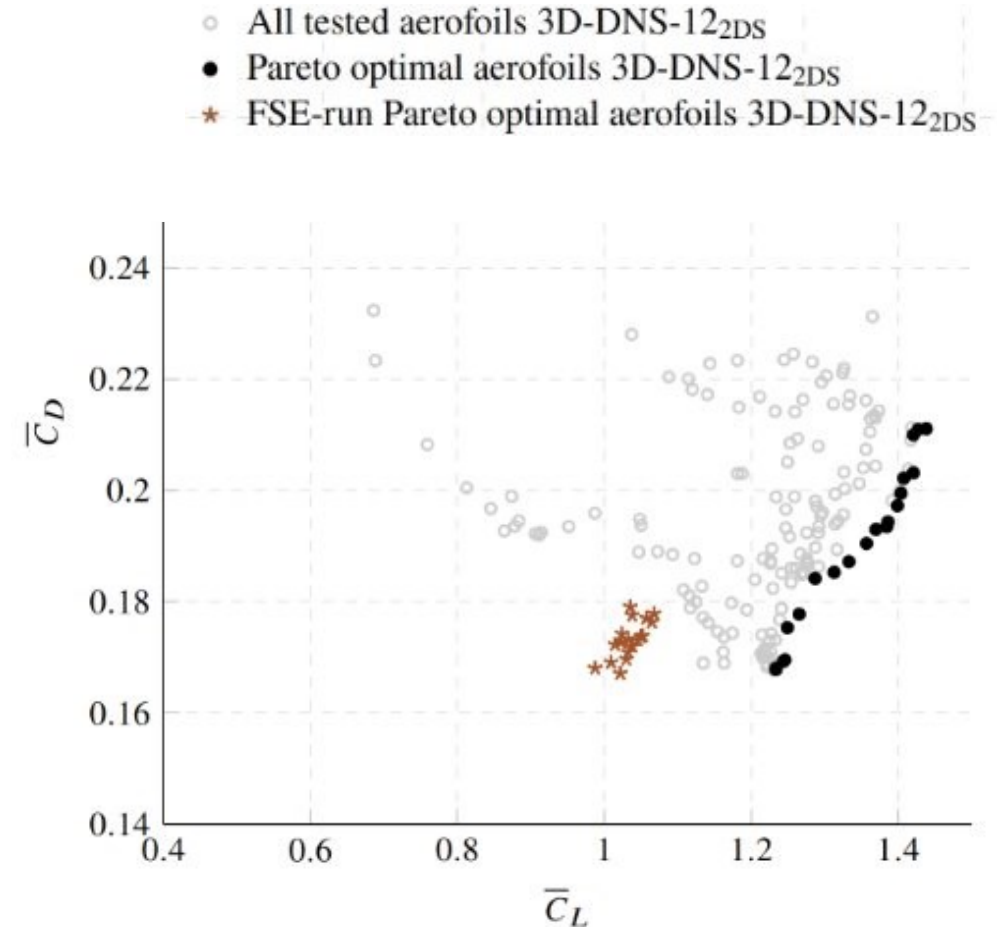
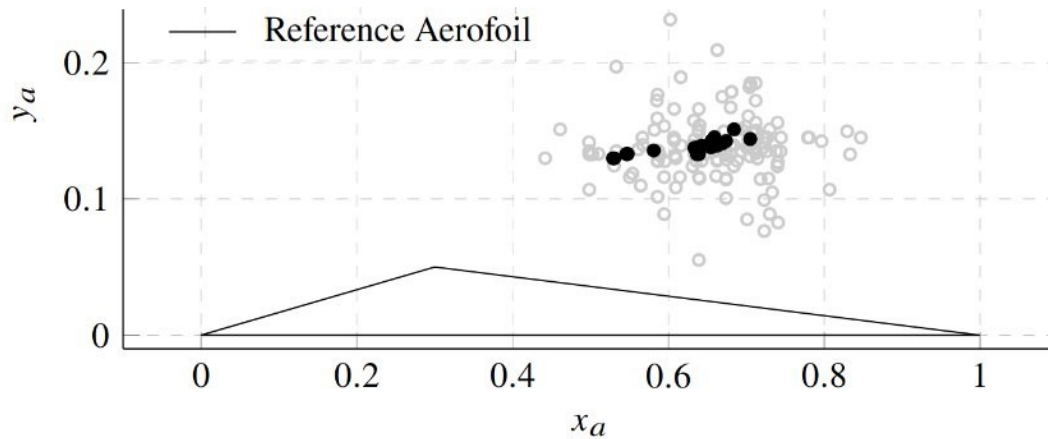
Free-stream eddies

TI=1% Is=0.1



# Optimisation with free-stream eddies

How would optimum airfoils look like if we optimised them with free-stream eddies?

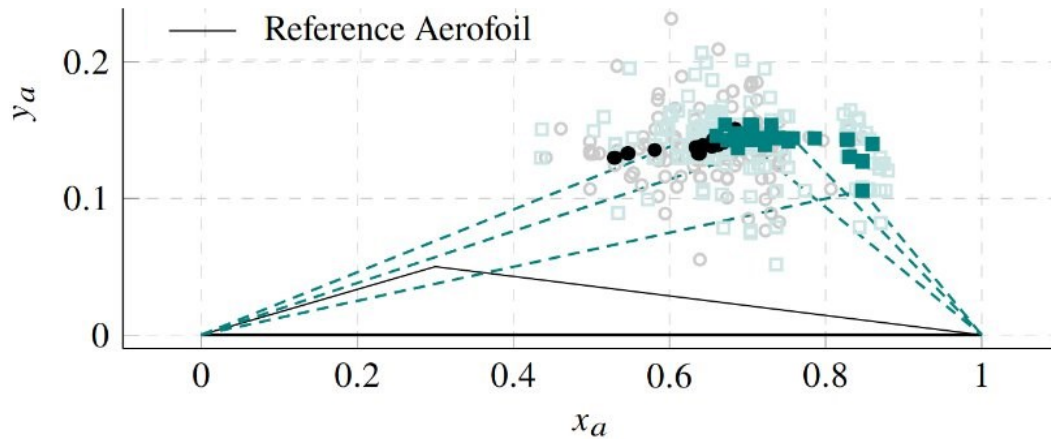


- All tested aerofoils 3D-DNS-12<sub>2DS</sub>
- Pareto optimal aerofoils 3D-DNS-12<sub>2DS</sub>
- ★ FSE-run Pareto optimal aerofoils 3D-DNS-12<sub>2DS</sub>

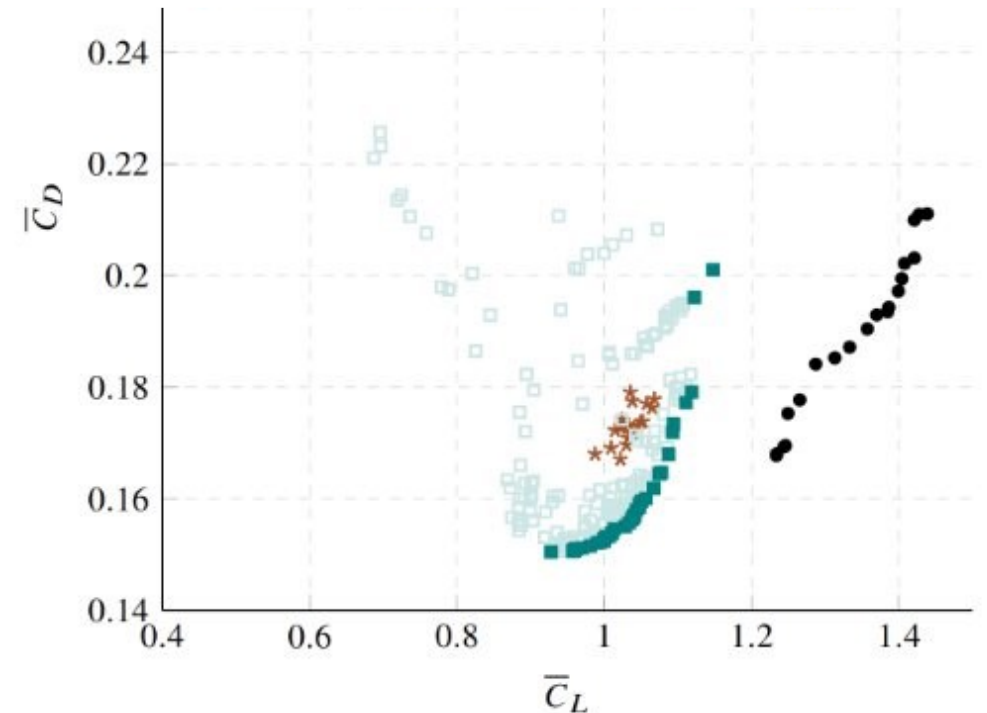


# Optimisation with free-stream eddies

- Optimum airfoils under free-stream eddies show apices towards the trailing edge.



- Pareto optimal aerofoils 3D-DNS-12<sub>2DS</sub>
- ★ FSE-run Pareto optimal aerofoils 3D-DNS-12<sub>2DS</sub>
- All tested aerofoils 3D-DNS-12-FSE<sub>3DS</sub>
- Pareto optimal aerofoils 3D-DNS-12-FSE<sub>3DS</sub>



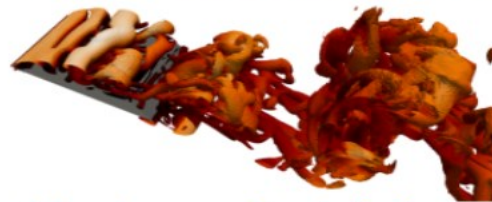
# Optimisation with free-stream eddies



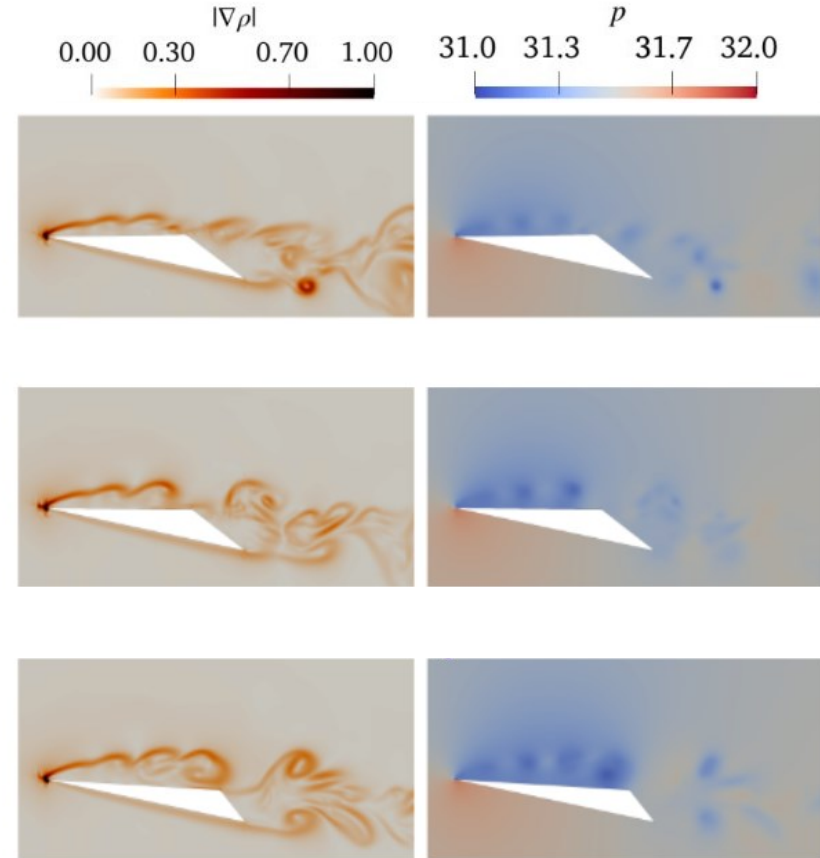
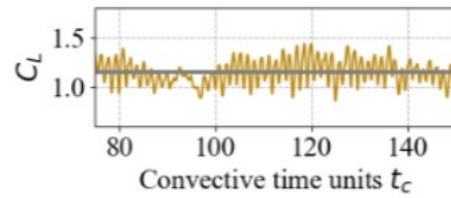
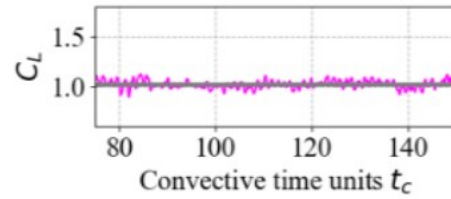
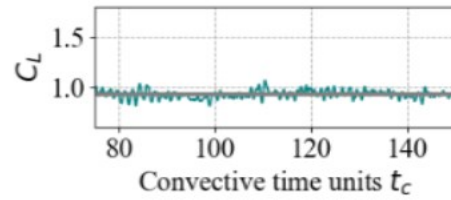
Minimum  $C_D$  airfoil



Maximum  $C_L/C_D$  airfoil

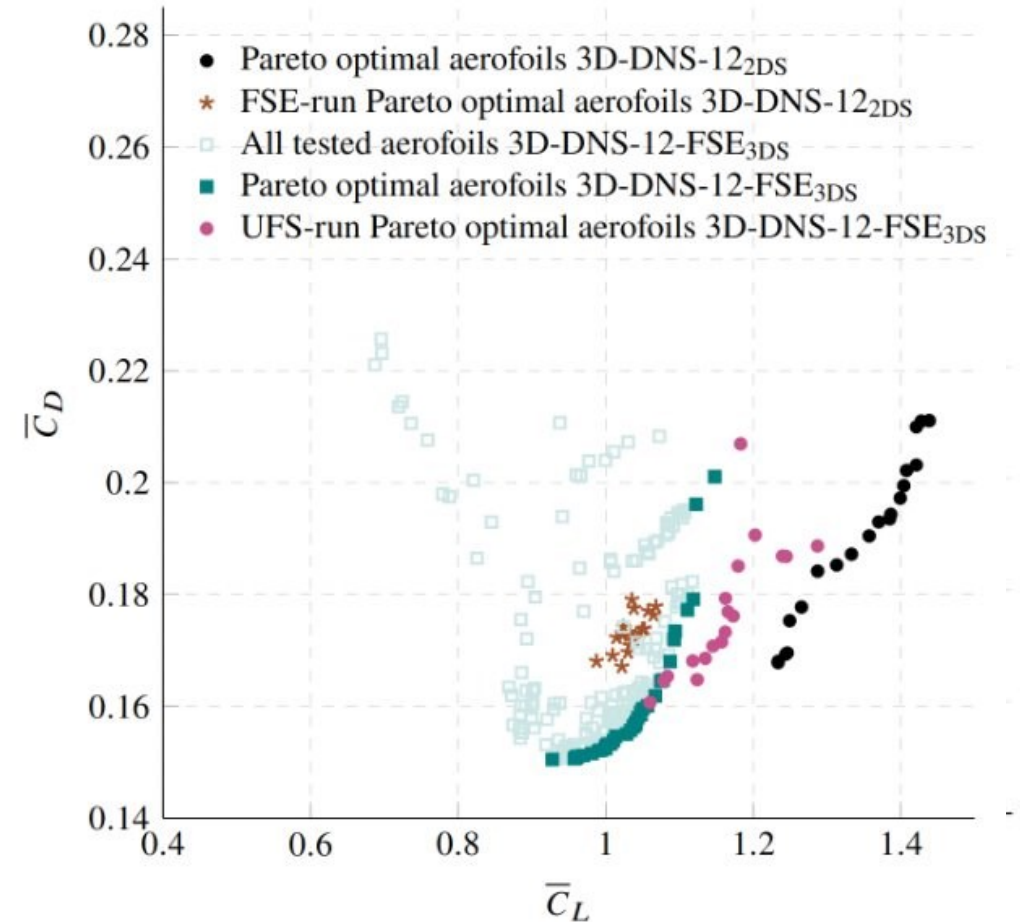
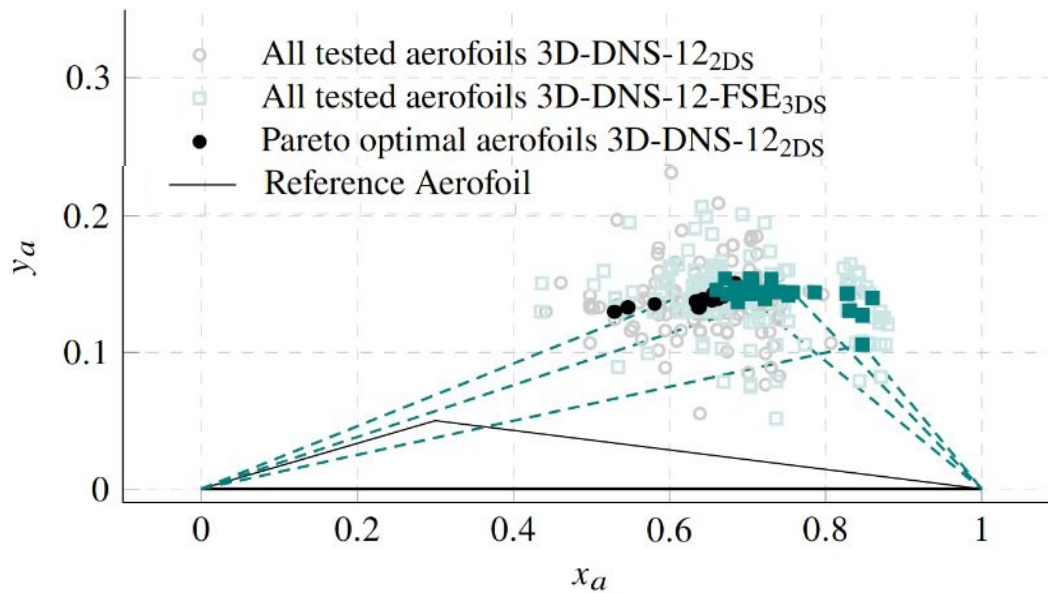


Maximum  $C_L$  airfoil



# Optimisation with free-stream eddies

- Pareto Front from optimisation with free-stream eddies run under **uniform free-stream conditions**
- **Multi-point** optimisation

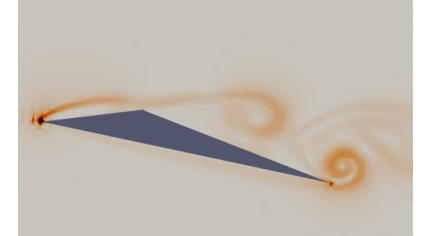


# Outline

- Introduction
- Optimisation setup
- Optimisation results
- Effects of free-stream eddies on optimised airfoils
- **Summary and Next Steps**

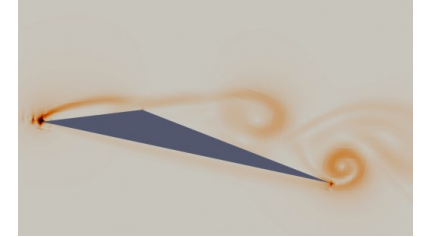
# Summary

- **Martian conditions** - low Reynolds number, high Mach number - **not typical on Earth**
  - Airfoils with **sharp leading edges** offer good performance – unexplored field
- **Optimisation** using high order accurate **DNS** with PyFR
  - Improved efficiency by **exploiting** the separation of the flow and **vortex roll-up**.
- **Effects of free-stream eddies**
  - Free-stream eddies **break** the **coherent structures** and **regularise performance** of different airfoils.
  - Optimised airfoils extend area to maximise the suction of vortex roll-up.



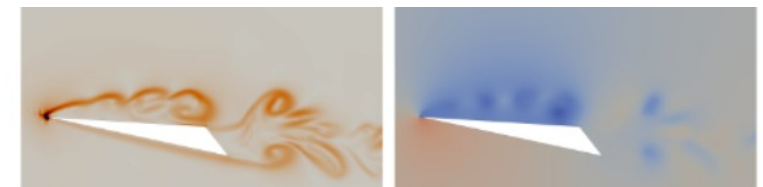
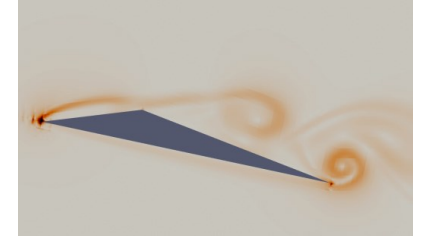
# Summary

- **Martian conditions** - low Reynolds number, high Mach number - **not typical on Earth**
  - Airfoils with **sharp leading edges** offer good performance – unexplored field
- **Optimisation** using high order accurate **DNS** with PyFR
  - Improved efficiency by **exploiting** the separation of the flow and **vortex roll-up**.
- **Effects of free-stream eddies**
  - Free-stream eddies **break** the **coherent structures** and **regularise performance** of different airfoils.
  - Optimised airfoils extend area to maximise the suction of vortex roll-up.



# Summary

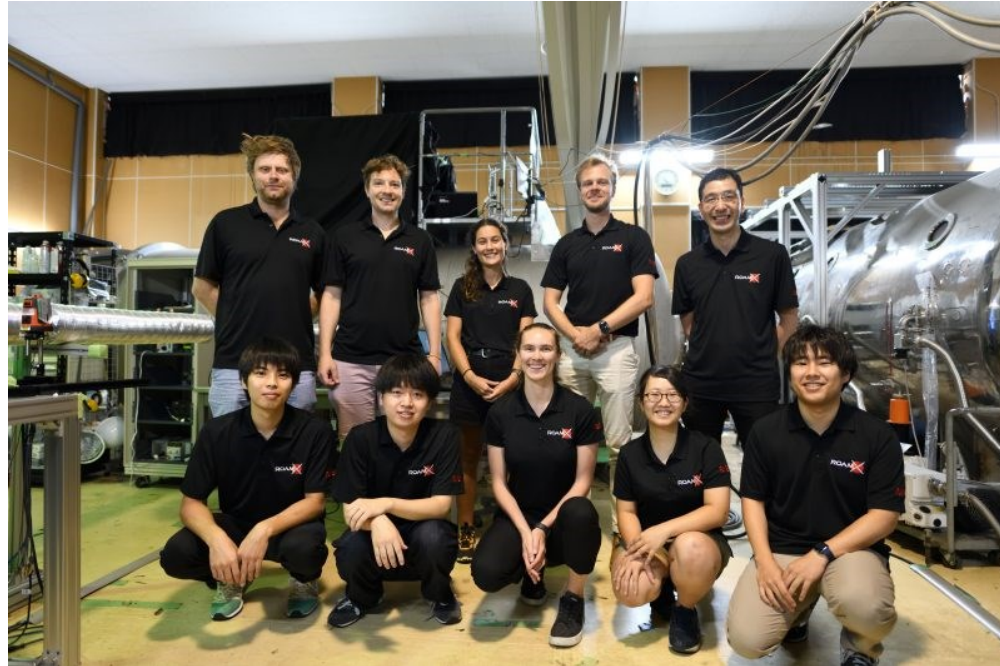
- **Martian conditions** - low Reynolds number, high Mach number - **not typical on Earth**
  - Airfoils with **sharp leading edges** offer good performance – unexplored field
- **Optimisation** using high order accurate **DNS** with PyFR
  - Improved efficiency by **exploiting** the separation of the flow and **vortex roll-up**
- **Effects of free-stream eddies**
  - Free-stream eddies **break** the **coherent structures** and **regularise performance** of different airfoils
  - Optimised airfoils extend area to **maximise the suction of vortex roll-up**



# Next Steps



IMPERIAL





# Acknowledgements



**CSCS**  
Centro Svizzero di Calcolo Scientifico  
Swiss National Supercomputing Centre



# Thank you

Lidia Caros Roca

Imperial College London

[lidia.caros-roca19@imperial.ac.uk](mailto:lidia.caros-roca19@imperial.ac.uk)